Carbon Dioxide Transport and Carbonic Anhydrase in Blood and Muscle

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I. Introduction

One of the major requirements of the body is to eliminate CO₂. The large, but highly variable, amount of CO₂ that is produced within muscle cells has to leave the body finally via ventilation by the lung. To get there, CO₂ diffuses from the intracellular space into the convective transport medium blood with the two compartments, plasma and erythrocytes. Within the body, CO₂ is transported in three different forms: physically dissolved, as HCO₃⁻, or as carbamate. The relative contribution of these three forms to overall transport changes markedly along this elimination pathway. Thus the kinetics of the interchange have to be considered. Carbonic anhydrase accelerates the hydration/dehydration reaction between CO₂, HCO₃⁻, and H⁺. In skeletal muscle, various isozymes of carbonic anhydrase are localized within erythrocytes but are also bound to the capillary wall, thus accessible to plasma; bound to the sarcolemma, thus producing catalytic activity within the interstitial space; and associated with the sarcoplasmatic reticulum. In some fiber types, carbonic anhydrase is also present in the sarcoplasm. In exercising skeletal muscle, lactic acid contributes huge amounts of H⁺ and by these affects the relative contribution of the three forms of CO₂. With a theoretical model, the complex interdependence of reactions and transport processes involved in CO₂ exchange was analyzed.

I. INTRODUCTION

One of the major requirements of the body is to eliminate CO₂. The large, but highly variable, amount of CO₂ that is produced within muscle cells has to leave the body finally via ventilation by the lung. To get there, CO₂ diffuses from the intracellular space into the convective transport medium blood, and diffusion out of the blood has to take place into the lung gas space across the alveolo-capillary barrier.

Carbon dioxide in the body is present in three different forms: dissolved, bound as bicarbonate, or bound as carbamate. The relative contribution of these different forms to overall CO₂ transport changes markedly along this elimination pathway, because for diffusion across membrane barriers, another form is more appropriate than for transport within intra- or extracellular compartments. Thus the kinet-
ics of the interchange between forms become critically important. In addition, the products of one such interchange, the hydration reaction of CO$_2$, HCO$_3^-$, and H$^+$, are required for a great variety of other cellular functions such as secretion of acid or base and some reactions of intermediary metabolism. In exercising skeletal muscle, the other “end product” of metabolism, lactic acid, contributes huge amounts of H$^+$ and by these affects the predominance of the three forms of CO$_2$, because HCO$_3^-$ as well as carbamate are critically dependent on the concentration of H$^+$. Discussion of the overall transport of CO$_2$ in skeletal muscle has to take into account this contribution of lactic acid and its involvement in kinetics and equilibria of CO$_2$ reactions. This interdependence of CO$_2$ and lactic acid elimination is one major aspect of this review, which as far as we know has not before been reviewed in detail.

II. CARBON DIOXIDE TRANSPORT IN BLOOD

A. Transport Forms of CO$_2$ in Blood

Carbon dioxide transport forms in blood have been thoroughly reviewed by Klocke (105). We only briefly summarize their respective contribution to overall CO$_2$ exchange. Table 1 sums up the contribution of the various forms in the two compartments plasma and erythrocytes: in whole arterial and venous blood during rest and during heavy exercise.

1. Dissolved CO$_2$

Only a small portion, ~5% of total arterial content, is present in the form of dissolved CO$_2$. Using a solubility coefficient S$_{CO2}$ of $3.21 \times 10^{-5}$ M/Torr (35) for plasma at 37°C, this gives 1.28 mM dissolved CO$_2$, or, using S$_{CO2}$ of $3.08 \times 10^{-5}$ M/Torr (7), 1.23 mM dissolved CO$_2$ at a P$_{CO2}$ of 5.32 kPa (40 Torr). At rest, the contribution of dissolved CO$_2$ to the total arterial CO$_2$ concentration difference is only ~10%. However, during heavy exercise, the contribution of dissolved CO$_2$ can increase sevenfold and then makes up almost one-third of the total CO$_2$ exchange.

2. CO$_2$ bound as HCO$_3^-$

The majority of CO$_2$ in all compartments is bound as HCO$_3^-$, as well as carbamate, which will be considered separately. The ratio of HCO$_3^-$ over dissolved CO$_2$ is given by the Henderson-Hasselbalch equation.

<table>
<thead>
<tr>
<th>TABLE 1. CO$_2$ transport in blood at rest and exercise</th>
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<tbody>
<tr>
<td><strong>Arterial</strong></td>
</tr>
<tr>
<td><strong>Plasma</strong></td>
</tr>
<tr>
<td><strong>pH†</strong></td>
</tr>
<tr>
<td>P$_{CO2}$</td>
</tr>
<tr>
<td>Dissolved</td>
</tr>
<tr>
<td>Carbamate</td>
</tr>
<tr>
<td>Sum plasma</td>
</tr>
<tr>
<td><strong>Red blood cell</strong></td>
</tr>
<tr>
<td><strong>pH†</strong></td>
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<td>Hb, g/l</td>
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<tr>
<td>Hct†</td>
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<tr>
<td>Hb$_{O2}$, fract†</td>
</tr>
<tr>
<td>Dissolved</td>
</tr>
<tr>
<td>Bicarbonate</td>
</tr>
<tr>
<td>Carbamate</td>
</tr>
<tr>
<td>Sum RBC</td>
</tr>
<tr>
<td>Total CO$_2$</td>
</tr>
</tbody>
</table>

Concentrations of the 3 forms of CO$_2$ in plasma and red blood cells (RBC) and their contribution to the concentrations in whole blood. Values of pH, P$_{CO2}$, hemoglobin (Hb), hematocrit (Hct), and fraction of O$_2$-saturated hemoglobin represent assumed standard values. Blood gas values for venous plasma during heavy exercise (*) were taken from Bangsbo et al. (6). Dissolved CO$_2$ was calculated using a solubility coefficient S$_{CO2}$ of 0.0308 mM/Torr. Bicarbonate was calculated using −log of the dissociation constant of $pK_a = 6.10$. Water content of erythrocytes was assumed to be 0.72, and extracellular pH (pHe) was calculated from pHe = 7.390 + (pH$_{plasma}$ + 1.644) as given by Hilpert et al. (85). Carbamate concentrations in plasma were calculated using the equilibrium constants given by Gros et al. (61). For the calculation of carbamate concentrations in erythrocytes, the equilibrium constants $pK_a$, $pK_b$, and $p$ from Gros et al. (68) were used with the exception of $pK_a$ (β-chain deoxy), which was calculated from $p$ of Perella et al. (135) and $pK_b$ (β-chain deoxy) of Gros et al. (68) to take into account the influence of 2,3-diphosphoglycerate concentration (see text). Units of mmol/l blood indicate contribution of the plasma and RBC, respectively, to the concentrations of each species to the concentration in whole blood. † Dimensionless quantities. v-a diff, arteriovenous difference.
The $pK_a$ has a normal value of 6.10 in human plasma at 37°C and varies with temperature and ionic strength (142). It appears to be slightly different in serum and red blood cells: serum, 6.11; oxygenated erythrocytes, 6.10; deoxygenated erythrocytes, 6.12 (8). During a heavy work load of the muscle, high levels of lactic acid are present in addition to CO$_2$, aggravating the decrease in pH. With this low pH, the fraction of HCO$_3^-$ in total CO$_2$ is diminished. Although at pH 7.4 HCO$_3^-$ is 20-fold compared with dissolved CO$_2$, it is only 13-fold at the normal intraerythrocytic pH of 7.2, and the ratio may fall to much lower values at plasma pH values of considerably below 7 during maximal exercise. Therefore, although the absolute arteriovenous difference is higher during exercise than during rest, the relative contribution of HCO$_3^-$ to overall exchange is less. For the example of heavy exercise given in Table 1, HCO$_3^-$ contributes only two-thirds of total CO$_2$ exchange, whereas at rest this figure is ~85%.

3. CO$_2$ bound as carbamate

The amount of CO$_2$ bound as carbamate to hemoglobin in erythrocytes or to plasma proteins depends on O$_2$ saturation of hemoglobin and 2,3-diphosphoglycerate (2,3-DPG) concentration in the case of erythrocytes, and on H$^+$ concentration in the case of both red blood cells and plasma (61, 68, 134, 135). During passage of blood through muscle, O$_2$ saturation and H$^+$ concentration change considerably, in particular during exercise. However, the increase in hemoglobin desaturation and the increase in H$^+$ concentration experienced by red blood cells in the capillary during exercise affect the amount of CO$_2$ bound to hemoglobin in opposite directions. Whereas deoxygenation of hemoglobin increases the amount of CO$_2$ bound to hemoglobin, acidification decreases the amount of carbamate formed by hemoglobin.

To calculate carbamate concentrations within erythrocytes, we use a single set of constants for the $\alpha$- and $\beta$-chains in the oxy state of hemoglobin and separate constants for the $\alpha$- and $\beta$-chains in the deoxy state. Because the calculation of carbamate is dependent on the values of the carbamate equilibrium constant ($pK_a$) and the ionization equilibrium constant of the amino group ($pK_z$) employed, errors in the determination of these constants in different studies can lead to changes in the calculation of the carbamate. Therefore, we use two different sets of constants to give an estimate of the variability of the calculated carbamate concentrations.

For oxyhemoglobin, we use the binding constants of Gros et al. (68) (number of CO$_2$ binding sites per hemoglobin tetramer $n = 2$, $pK_a = 4.73$, $pK_z = 7.16$), and for deoxyhemoglobin, their constants for the $\alpha$-chain $\alpha$-amino groups of $n = 2$, $pK_a = 5.19$, $pK_z = 7.05$. However, because their measurements were done in the absence of 2,3-DPG, their carbamate equilibrium constant ($K_d$) for the $\alpha$-amino groups of the $\beta$-chains of deoxyhemoglobin was not used. On the other hand, intraerythrocytic concentration of 2,3-DPG has effectively no influence on the binding of CO$_2$ to oxyhemoglobin and to the $\alpha$-chain $\alpha$-amino groups of deoxyhemoglobin (132). For the $\beta$-chain $\alpha$-amino groups of deoxyhemoglobin, the ionization constant ($K_d$; $pK_z = 6.13$) estimated by Gros et al. (68) was used in conjunction with the CO$_2$ binding constant $\lambda$ for this same amino group given by Perella et al. (135) for the presence of 2,3-DPG. Perella et al. (135) determined this figure by measuring CO$_2$ binding of hemoglobin whose $\alpha$-amino groups were differentially blocked by cyanate. Using their value of $\lambda$, one obtains together with the above value of $pK_z$ a carbamate equilibrium constant $pK_a = 5.06$ for these groups. Thus we describe CO$_2$ binding by the $\alpha$-amino groups of the $\beta$-chains of deoxyhemoglobin in the presence of 2,3-DPG with $n = 2$, $pK_a = 6.13$, and $pK_z = 5.06$. With these constants we estimate a contribution of only ~5% (0.09 mM) of carbamate to overall CO$_2$ exchange during rest (Table 1). When the $pK_a$ and $pK_z$ values reported by Perella et al. (134) and the data of Perella et al. (135) are combined in an analogous fashion to estimate binding constants in the presence of 2,3-DPG, a contribution of 9% (0.16 mM) of carbamate to CO$_2$ exchange during rest is calculated. The former estimate of 0.09 mM or 5% agrees nicely with measurements of Böning et al. (13). From their data, an arteriovenous difference for carbamate of 0.09 mM is calculated for the blood gas values of Table 1. It should be noted that all these estimates of the contribution of carbamate to overall CO$_2$ exchange are lower than the value of 12.6% calculated by Klocke (105). However, Klocke's use of the data of Perella et al. (135), which are valid for pH 7.4 rather than the normal intraerythrocytic pH 7.2, may have led to a substantial overestimate of the role of carbamate because carbamate formation increases drastically with increasing pH. Thus it appears that a contribution of 5% by carbamate is a reasonable estimate although markedly lower than previously believed.

During heavy exercise as defined in Table 1, ~6% (10.8% with the data of Perella and co-workers, Refs. 134, 135) of the arteriovenous concentration difference of total CO$_2$ is calculated to be due to a change in carbamate. Böning et al. (13) have measured an ~10% contribution to overall exchange during aerobic exercise, but during heavy exercise with considerable anaerobic metabolism they found that carbamate does not contribute to CO$_2$ exchange at all; arterial blood contained a carbamate concentration that was higher by 0.06–0.13 mol/mol hemoglobin than that of venous blood in the presence of lactic acid. The data of Table 1 thus represent an inter-
mediate position between these extreme types of exercise.

Carbamate concentration in plasma does not contribute to overall CO₂ exchange according to Table 1, which is in agreement with Klocke’s conclusion (105). During heavy exercise, arterial plasma contains an even higher concentration of carbamate than venous plasma. The physicochemical reason for this is that, in the absence of an oxylabile carbamate fraction as exhibited by hemoglobin, the increase in carbamate by the elevated P<sub>CO₂</sub> in venous plasma is counteracted or overruled by a decrease in carbamate caused by the fall in pH.

B. Transport Within the Intracellular Compartment

Figure 1 shows that overall CO₂ transport is the sum of the diffusion of 1) dissolved CO₂ and 2) CO₂ bound as HCO₃⁻. The contribution of HCO₃⁻ to CO₂ transport is called “facilitated CO₂ diffusion” and was first described by Longmuir et al. (111). Gros and Moll (66) and Gros et al. (67) have shown that facilitated CO₂ diffusion involves a flux of H⁺ equivalent to that of HCO₃⁻, a fact which matches the other fact that hydration of CO₂ produces equal amounts of H⁺ and HCO₃⁻. Facilitated CO₂ diffusion by HCO₃⁻ diffusion under steady-state conditions then requires 1) rapid conversion of CO₂ into HCO₃⁻ and H⁺, which at the short diffusion distances as they occur in cells (<1 mm) implies that the presence of carbonic anhydrase (CA) catalyzing CO₂ hydration is essential for facilitation to occur, and 2) equal fluxes of H⁺ and HCO₃⁻, where 3) significant fluxes of H⁺ can only be achieved when they occur by facilitated H⁺ diffusion, i.e., by the diffusion of mobile buffers carrying H⁺ and present at concentrations comparable to that of HCO₃⁻. This leads to the following scheme of facilitated CO₂ diffusion shown in Figure 1.

![Mechanism of facilitated diffusion of CO₂](image)

**FIG. 1.** Mechanism of facilitated diffusion of CO₂. White background area indicates free diffusion (physically dissolved) CO₂, and the shaded background indicates the process of facilitated CO₂ diffusion. “Buffer” is any mobile buffer with an appropriate pK value, such as phosphate at pH 7.

### Table 2. Diffusion coefficient of dissolved CO₂ in water and hemoglobin solutions

<table>
<thead>
<tr>
<th>Medium</th>
<th>Temperature, °C</th>
<th>Diffusion Coefficient, cm²/s</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>22</td>
<td>1.71 x 10⁻⁵</td>
<td>Gros and Moll (64)</td>
</tr>
<tr>
<td>16 g% Hemoglobin</td>
<td>38</td>
<td>2.5 x 10⁻⁵</td>
<td>Gros and Moll (64)</td>
</tr>
<tr>
<td>33 g% Hemoglobin</td>
<td>38</td>
<td>1.6 x 10⁻⁵</td>
<td>Gros and Moll (64)</td>
</tr>
<tr>
<td>100% Hemolysate</td>
<td>37</td>
<td>0.34 x 10⁻⁵</td>
<td>Uchida et al. (173)</td>
</tr>
</tbody>
</table>

1. Diffusion of dissolved CO₂

Diffusion coefficients (=diffusion constant/S<sub>CO₂</sub>) have been measured under conditions where only little facilitated diffusion is present. In a 33g% hemoglobin solution, the hemoglobin concentration that prevails inside the red blood cell, the CO₂ diffusion coefficient, is reduced to less than one-half of its value in water (Table 2). It is not clear why the figure of Uchida et al. (173) is three times lower than the figure of Gros and Moll (64) for this condition. Compared with diffusion in water, diffusion is hindered by the presence of hemoglobin as it is by the presence of other intracellular proteins. It appears that proteins are virtually impermeable to CO₂ and represent the major obstacles to CO₂ diffusion within cells (64). Accordingly, CO₂ diffusion constants decrease in a defined manner with increasing hemoglobin concentration (curve in Fig. 2) that can be explained quantitatively on the basis of the geometry of the water space in a hemoglobin solution (64). Similarly, the CO₂ diffusion constant in various tissues varies systematically with the protein concentration of these tissues (points in Fig. 2). It is obvious that, for a given protein concentration, the CO₂ diffusion constants in these different cells or tissues agree very nicely.

2. Diffusion of HCO₃⁻

The diffusion coefficients for HCO₃⁻ are about one-half as great as those for CO₂, and in the presence of proteins, its diffusion can be expected to be hindered to an extent comparable to that observed for CO₂ diffusion. The HCO₃⁻ diffusion coefficient is calculated from the equivalent conductivity of HCO₃⁻ (67, 108), 11.7 x 10⁻⁶ cm²/s in pure water at 25°C, and is reduced to 8.7 x 10⁻⁶ cm²/s at physiological ionic strength and 25°C (67). Again, Uchida et al. (173) report a surprisingly low value of 1.4 x 10⁻⁶ cm²/s for HCO₃⁻ diffusion in “100% hemolysate” at 37°C. The relative contribution of HCO₃⁻ to total CO₂ diffusion (=facilitated diffusion) can be evaluated on the basis of these diffusion coefficients. The contribution of HCO₃⁻ diffusion, and thus of facilitated diffusion, to total CO₂ diffusion depends greatly on the partial pressure.
range of CO₂ in which the transport process takes place. This can be predicted from the general shape of CO₂ binding curves, which are steep at low PCO₂ values and become flatter with increasing PCO₂. Therefore, the HCO₃⁻ concentration gradient per CO₂ concentration gradient is higher at low PCO₂, and vice versa. This implies that the relative contribution of facilitated diffusion is highest at lowest PCO₂ values and decreases consistently with increasing PCO₂ (66, 67).

3. Diffusion of H⁺

The diffusion coefficient of free H⁺ in aqueous solutions at 25°C is 9.3 × 10⁻⁵ cm²/s (123), i.e., H⁺ possess a more than five times greater diffusivity in water than CO₂. Nevertheless, free diffusion of H⁺ is a rather ineffective mechanism of H⁺ transport, because at physiological values of pH, the H⁺ concentration gradients within cells cannot exceed the order of 10⁻⁷ to 10⁻⁸ M. In the presence of buffering substances at physiological concentrations of 10⁻³ to 10⁻² M, such differences of free H⁺ concentrations are accompanied by concentration differences of buffered H⁺ of at least of 10⁻³ to 10⁻² M or more. This very much higher concentration difference of the bound H⁺ compensates for the lower diffusion coefficients of mobile buffers. The diffusion coefficient for a mobile buffer such as phosphate is of the same order of magnitude as that of HCO₃⁻, 7.0 × 10⁻⁵ cm²/s (67). Consider as an example an intracellular pH difference of 0.1 between absolute pH values of 7.1 and 7.2; then, the expected flux of H⁺ by free H⁺ diffusion, estimated as diffusion coefficient (D) × concentration difference (Δc), gives 9.3 × 10⁻⁵ × 1.62 × 10⁻⁸ mmol-cm⁻¹ s⁻¹ = 1.5 × 10⁻¹² mmol-cm⁻¹ s⁻¹. Estimating facilitated H⁺ flux by diffusion of buffered H⁺ with the assumption of a buffer capacity of 40 mM/ΔpH and the above value of D for phosphate in an analogous fashion yields 7.0 × 10⁻⁶ × 0.1 × 40 × 10⁻³ mmol-cm⁻¹ s⁻¹ = 2.8 × 10⁻⁸ mmol-cm⁻¹ s⁻¹. Thus facilitated H⁺ diffusion by buffer diffusion in this example is more than 10,000 times more effective than free diffusion of H⁺. It has been shown that not only the diffusion of low-molecular-weight buffers such as phosphate (67) but also the diffusion of protein buffers (66) is a highly effective means of H⁺ transport. In the case of very large protein molecules, it has even been shown that facilitated H⁺ transport occurs very efficiently not only by translational but in addition by rotational protein diffusion (62, 63). Thus facilitated CO₂ diffusion essentially occurs by diffusion of HCO₃⁻ and simultaneous buffer-facilitated H⁺ diffusion. That buffer mobility is indispensable for this process to take place has been shown by Gros et al. (67) by demonstrating that immobilized phosphate buffer cannot entertain facilitated CO₂ diffusion.

Al-Baldawi and Abercrombie (3) have reported measurements of H⁺ diffusion in cytoplasm extracted from giant neurons of a marine invertebrate. An apparent diffusion coefficient for H⁺ of only 1.4 × 10⁻⁶ cm²/s was determined, which was 5 times lower than the estimated diffusion coefficient of the mobile buffers and 70 times lower than the diffusion coefficient of free H⁺. This appears to be in contradiction to the above considerations. However, because the authors performed their measurements under non-steady-state conditions by observing the relaxation of pH after a sudden pH change at one surface of the cytoplasm sample, it appears likely that this value represents a substantial underestimate of the apparent H⁺ diffusivity that one would observe under steady-state conditions. A pH transient will be greatly slowed down by
the presence of buffers whose buffering capacity is so overwhelming compared with free H⁺ concentration. This problem was aggravated in the experiments of Al-Baldawi and Abercrombie (3) by the presence in the cytoplasm of a substantial fraction of immobile buffers.

The contribution of facilitated diffusion to overall diffusion depends on the actual concentration differences for HCO₃⁻ and for buffered H⁺. These in turn are dependent on the actual pH gradient and the pK value(s) of the mobile buffer(s) present. As an example, calculated CO₂ fluxes are shown in Figure 3 as a function of the average pH with boundary PO₂ values of 5.32 and 6.65 kPa (40 and 50 mmHg) in a 66 mM phosphate solution (pK 6.84, 25°C). Total CO₂ diffusion is more than twice as high as free diffusion of dissolved CO₂ in a pH range of ~6.9–7.8. Thus more than one-half of the CO₂ transport in this model system occurs by facilitated diffusion, which means that at a physiological pH of the intracellular or extracellular spaces more HCO₃⁻ than CO₂ molecules contribute to total CO₂ flux within the compartment. Facilitated diffusion does not reach its maximum exactly at the pK value of the phosphate, i.e., at the maximal buffer capacity of the solution. The reason for this is that whereas above pH 6.84 the buffer capacity decreases, the pH difference across the layer increases markedly. The sum of these two effects leads to an increase with increasing pH in the concentration differences of HCO₃⁻ and of the H⁺-carrying H₂PO₄⁻ beyond the pK of the phosphate buffer. Under physiological conditions, the course of this curve may be different, since buffering is accomplished by different sets of buffers with more than one pK value. Although proteins, which are important buffers in intact cells, possess a lower diffusivity than inorganic phosphate, their large buffer capacity for H⁺ results in a facilitation of CO₂ diffusion in intact cells that is of a similar order of magnitude as shown in Figure 3 for phosphate. For the condition within red blood cells, in a hemoglobin solution of 30 g% Hb at 38°C and at roughly physiological pH and PO₂, Gros and Moll (65) have measured a contribution of facilitated CO₂ diffusion of ~85% to total intraerythrocytic CO₂ transport.

C. Transport Across the Erythrocyte Membrane

Although total CO₂ flux across the membrane can again be considered as the sum of diffusion of dissolved CO₂ and of HCO₃⁻ with accompanying H⁺, the relative contributions of dissolved and bound CO₂ to overall CO₂ flux across the erythrocyte membrane are quite different compared with diffusion within the intracellular compartment.

1. Dissolved CO₂

Cell membranes are generally considered to be highly permeable to gases such as CO₂ or O₂, with one of the few exceptions being the apical membrane of parietal and chief cells of gastric glands, which have been described to possess “no detectable permeability to NH₃, NH₄⁺, CO₂, and HCO₃⁻” and whose surface area times permeability product was found to be about three orders of magnitude lower than that of the basolateral membranes of the same cells (15, 176). Erythrocyte membranes, though, are highly permeable to CO₂, the absolute permeability values cited being in the range of 0.35–3 cm/s (Table 3), as has been thoroughly discussed by Klocke (105). More recently, Forster et al. (47) measured the rate of depletion of C¹⁸O¹⁸O in erythrocyte suspensions by mass spectroscopy. They evaluated their measurements...
TABLE 4. Permeability of erythrocytic and other membranes

<table>
<thead>
<tr>
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<th>Permeability, cm/s</th>
<th>References</th>
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<tr>
<td>CO₂</td>
<td>Extrapolated, from NH₃ measurements, erythrocytic membrane</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>Calculated from comparison of diffusion in hemoglobin solution vs. red cell suspension</td>
<td>&gt;3.0</td>
</tr>
<tr>
<td>Lipid bilayer</td>
<td></td>
<td>0.35</td>
</tr>
<tr>
<td></td>
<td>Calculated from comparison of diffusion in hemoglobin solution vs. red cell suspension</td>
<td>1.6</td>
</tr>
<tr>
<td>Red blood cells, mass spectrometry</td>
<td></td>
<td>−1</td>
</tr>
<tr>
<td>HCO₃⁻</td>
<td>Phospholipid vesicles, 25°C</td>
<td>4.3 × 10⁻⁶</td>
</tr>
<tr>
<td></td>
<td>Frog skeletal muscle, room temperature</td>
<td>2 × 10⁻⁷</td>
</tr>
<tr>
<td></td>
<td>Human erythrocytic membrane, 37°C</td>
<td>5.6 × 10⁻⁴</td>
</tr>
<tr>
<td></td>
<td>H⁺/OH⁻</td>
<td>Phospholipid vesicles, 25°C</td>
</tr>
<tr>
<td></td>
<td>Erythrocytic membrane, at pHₑ 7.4, 37°C</td>
<td>2.4 × 10⁻³</td>
</tr>
</tbody>
</table>

pHₑ, extracellular pH.

to give the CO₂ permeability of the human red cell membrane and obtained a value of ~1 cm/s. If we simplistically equate physiological CO₂ concentration with CO₂ concentration difference across the membrane (cₐ in CO₂), we can estimate the possible order of magnitude of physiologically occurring CO₂ fluxes from Pₐ in CO₂ × cₒ in CO₂ = 1 cm/s × 1 mM = 1 × 10⁻³ mmol·cm⁻²·s⁻¹.

2. HCO₃⁻

Permeability for HCO₃⁻ of artificial phospholipid vesicles, which are devoid of any anion exchanger, is six orders of magnitude lower (Table 3; Ref. 127) than it is for dissolved CO₂. However, erythrocyte membranes of all vertebrates with the exception of agnathans (hagfishes and lampreys; see reviews, Refs. 80, 126, 136) do have a rapid anion (HCO₃⁻/Cl⁻) exchange protein, capnophorin or band 3 (see review by Jennings, Ref. 90), which exchanges HCO₃⁻ for Cl⁻ at a ratio of 1:1. An overview of the distribution of this transporter in red blood cells is given in Table 4. Thus the permeability of the erythrocyte membrane to HCO₃⁻ is considerably increased over that of lipid bilayers but still about three to four orders of magnitude lower than the permeability for dissolved CO₂ (Table 3).

Net driving force for HCO₃⁻/Cl⁻ exchange is proportional to the difference in the electrochemical potential for both ions. The turnover number of this transporter is 4–5 × 10⁴ Cl⁻·s⁻¹·molecule⁻¹ at 37°C (16, 56). With this figure and the number of 1.0–1.2 × 10⁶ copies of capnophorin per red blood cell (90), a maximal flux across the membrane of ~6 × 10⁻⁵ mmol·cl⁻·cm⁻²·s⁻¹ can be calculated using an erythrocytic volume of 80 × 10⁻¹² cm³ and a red cell surface of 1.6 × 10⁻⁶ cm². Maximal HCO₃⁻ flux is expected to be in the same range as that of Cl⁻. Flux measurements at 0°C have shown a maximal value for HCO₃⁻ flux of 1% of this theoretical value, ~5 × 10⁻⁷ mmol·HCO₃⁻·cm⁻²·s⁻¹ (48). When the large temperature dependence of the anion transporter with a turnover number at 0°C of only ~200 Cl⁻·s⁻¹·molecule⁻¹ (56) is taken into account, this agrees well with the value calculated above for maximal flux at 37°C. Values of HCO₃⁻ permeability of erythrocyte membranes are similar for humans and birds (as well as in several other species). In red blood cells of adult humans and of chicken HCO₃⁻ permeability (Pₐ in HCO₃⁻) was measured to be 5.6 × 10⁻⁴ and

TABLE 4. Carbonic anhydrase activity and HCO₃⁻/Cl⁻ exchanger in blood of different species

<table>
<thead>
<tr>
<th></th>
<th>Plasma</th>
<th>Red Blood Cell</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>CA available to plasma</td>
<td>CA in plasma</td>
</tr>
<tr>
<td>Mammals (human, dog, rat, rabbit, mouse)</td>
<td>+Lung</td>
<td>−</td>
</tr>
<tr>
<td></td>
<td>+Muscle</td>
<td>−</td>
</tr>
<tr>
<td>Dog, pig, sheep, rabbit</td>
<td>−</td>
<td>+</td>
</tr>
<tr>
<td>Ox, domestic cat, lion, jaguar, tiger, leopard</td>
<td>−</td>
<td>+</td>
</tr>
<tr>
<td>Birds (chicken)</td>
<td>−</td>
<td>+</td>
</tr>
<tr>
<td>Amphibian (frog)</td>
<td>−</td>
<td>+</td>
</tr>
<tr>
<td>Teleosts (trout, eel, flounder)</td>
<td>+Gill</td>
<td>+</td>
</tr>
<tr>
<td>Trout</td>
<td>+Muscle</td>
<td>+</td>
</tr>
<tr>
<td>Elasmobranchs (dogfish)</td>
<td>+Gill</td>
<td>+</td>
</tr>
<tr>
<td>Agnathans (hagfish, lamprey)</td>
<td>−Gill</td>
<td>+</td>
</tr>
</tbody>
</table>

Carbonic anhydrase (CA) I and CA II, respectively, or isozymes are functionally similar to these mammalian isozyymes. Data were taken from the following references: a 113; b 83, 109; c 115; d 74, 75, 136; e 186; f 129; g 39, 131, 171, 172; h review, 11; i 25, 37, 128, 175, 179, 180; j 82; k 79; l 167; m 18; n 28; o 114.
7 \times 10^{-4} \text{ cm/s}, respectively (160). These latter authors showed that a functionally active band 3 protein is present in the erythrocyte membrane of the chicken at very early stages of development. In the dogfish (Mustelus canis), flux of HCO$_3^-$ across red cell membrane was reported to equal flux across human red cell membranes (128). It should be mentioned that a very large number of measurements have been reported for the HCO$_3^-$ permeability of the human red blood cell (e.g., Refs. 19, 30, 88, 103), most of which yielded numbers very similar to that of Sieger et al. (160), as cited in Table 3. Estimating the physiologically possible HCO$_3^-$ flux across the red cell membrane in a fashion analogous to that used above for CO$_2$, one obtains the following: 

\[ P_{\text{HCO}_3^-} \times c_{\text{HCO}_3^-} = 5 \times 10^{-4} \text{ cm/s} \times 10 \text{ mM} = 5 \times 10^{-6} \text{ mmol cm}^{-2} \text{s}^{-1}, \] 

which is \( \sim 10 \) times less than the maximal flux of \( 6 \times 10^{-5} \text{ mmol cm}^{-2} \text{s}^{-1} \) estimated above from turnover number and number of copies of capnophorin per red blood cell but more than two orders of magnitude smaller than the above CO$_2$ flux.

3. H$^+$

Proton permeability of phospholipid vesicles is five times higher than HCO$_3^-$ permeability, \( 1.8 \times 10^{-5} \text{ cm/s} \) (127). However, because the H$^+$ concentration gradient across the cell membrane is very small (intracellular pH 7.2, extracellular pH 7.4, \( \Delta \text{pH} 0.2 \)), the product permeability \( \times \) concentration gradient, is also very small: 

\[ P_{\text{H}^+} \times c_{\text{H}^+} = 1.8 \times 10^{-5} \text{ cm/s} \times 2.3 \times 10^{-8} \text{ M} = 4 \times 10^{-13} \text{ mmol H}^+ \text{cm}^{-2} \text{s}^{-1}. \]

Thus diffusion of free H$^+$ across the membrane is so small that it cannot support any facilitated CO$_2$ diffusion. However, in addition to free H$^+$ diffusion, there are several other more efficient mechanisms of H$^+$ transport across the red cell membrane. The significance of these pathways for overall H$^+$ flux across the erythrocytic membrane depends on the specific conditions. Proton fluxes (or reverse OH$^-$ fluxes) in erythrocyte membranes can be achieved via 1) the Jacobs-Stewart cycle, which includes HCO$_3^-/Cl^-$ exchange via capnophorin; 2) H$^+$ flux via HCl cotransport (or OH$^-$/Cl$^-$ countertransport); and 3) H$^+$ flux via H$^-$/lactate cotransport and nonionic lactic acid diffusion.

Bisognano et al. (12) measured H$^+$ fluxes across red cell membranes by a pH stat method. They induced these fluxes by establishing an outward Cl concentration gradient through increasing the osmotic strength of the extracellular solution with sucrose. Without lactate/lactic acid present, two-thirds of the measured apparent H$^+$ flux was mediated via the Jacobs-Stewart cycle (89), and one-third was due to a DIDS-sensitive HCl cotransport. The Jacobs-Stewart cycle brings about a H$^+$ efflux from the red blood cell by the following sequence of processes: 1) H$^+$ in the cell reacts with HCO$_3^-$ to give CO$_2$, 2) CO$_2$ leaves the cell and 3) is hydrated extracellularly to give H$^-$ and HCO$_3^-$. Where 4) the H$^-$ remains outside while the HCO$_3^-$ enters the cell in exchange for Cl$^-$ via the Cl$^-$/HCO$_3^-$ exchanger.

Bisognano et al. (12) base their study on the assumption that the Jacobs-Stewart cycle-mediated H$^+$ flux is inhibitable by the CA inhibitor ethoxzolamide, whereas HCl cotransport is not affected by this drug but suppressed by DIDS. Under their conditions, an initial flux via HCl cotransport was observed at \( 0.5 \times 10^{-9} \text{ mmol H}^+ \text{cm}^{-2} \text{s}^{-1} \), compared with \( 1 \times 10^{-9} \text{ mmol H}^+ \text{cm}^{-2} \text{s}^{-1} \) mediated by the Jacobs-Stewart cycle, giving a total H$^+$ flux by these two mechanisms of \( 1.5 \times 10^{-9} \text{ mmolcm}^{-2} \text{s}^{-1} \).

Compared with free H$^+$ diffusion, this value is very high; it is considerably lower than the HCO$_3^-$ flux estimated above and substantially lower than the estimated CO$_2$ flux.

A third mechanism of H$^+$ transport across the red cell membrane is by the H$^+$/lactate carrier and by nonionic diffusion of lactic acid, both of which require the presence of lactate (27, 138). Proton fluxes via this mechanism were calculated from flux measurements of Fishbein et al. (42) and of Poole and Halestrap (138) in human red blood cells to be \( 2-2.5 \times 10^{-11} \text{ mmol H}^+ \text{cm}^{-2} \text{s}^{-1} \). Thus, in the presence of lactate, the above H$^+$ flux estimate would have to be raised to \( \sim 4 \times 10^{-9} \text{ mmolcm}^{-2} \text{s}^{-1} \), which is much lower than the flux estimate for HCO$_3^-$. The fluxes of both ions, however, are more than two orders of magnitude smaller than a physiological CO$_2$ flux. Thus a significant facilitation of CO$_2$ diffusion across the red cell membrane does not occur. It may be noted that the activity of the H$^+$/lactate cotransport can be increased considerably in Plasmodium falciparum-infected human erythrocytes (96).

In conclusion, the permeability of dissolved CO$_2$ is much greater than the effective permeability of HCO$_3^-$ and H$^+$. At the same time, more than two-thirds of the CO$_2$ transported in either red blood cells or plasma is transported in the form of HCO$_3^-$. This makes it appear essential that CO$_2$ and HCO$_3^-$ can be converted into each other quite rapidly at the boundary between the two compartments: intracellular and plasma. A high velocity of this interconversion is achieved by the enzyme CA.

Although HCO$_3^-$ and H$^+$ are produced in equal amounts by the hydration of CO$_2$, the distribution of the two products among the two compartments, intracellular and plasma, is quite different at electrochemical equilibrium. Bicarbonate is transported to a larger fraction within plasma than within erythrocytes because the equilibrium pH of the plasma is more alkaline than the intracellular pH (Table 1). In contrast, H$^+$ are transported to a larger fraction within erythrocytes than in plasma because the nonbicarbonate buffer capacity of erythrocytes exceeds that of plasma by a factor of \( \sim 10 \).

The CO$_2$ entering the blood during capillary passage through the peripheral tissue can encounter two different situations: 1) a situation where CA is present in red blood...
cells only, or 2) a situation where CA is available in red blood cells and in plasma,

A) Rapid catalysis occurs only within erythrocytes. Carbon dioxide enters the red blood cells, and there is rapidly converted to HCO$_3^-$ and H$^+$. When the red blood cell has reached the end of the capillary, electrochemical equilibrium across erythrocyte membrane is not yet established, because H$^+$ concentration and even more so HCO$_3^-$ concentration are too high within red blood cells compared with plasma concentrations. A significant fraction of the intraerythrocytic HCO$_3^-$ has left the cell via HCO$_3^-$/Cl$^-$ exchange already during capillary transit. After blood has left the capillary, part of HCO$_3^-$ and H$^+$ that has been produced within the red blood cell is dehydrated back to give CO$_2$; CO$_2$ then leaves the cell and enters the plasma, where the slow uncatalyzed reaction hydrates CO$_2$ to establish final equilibrium. During this postcapillary process, the plasma pH shifts slowly in the acidic direction.

B) Rapid catalysis occurs in erythrocytes and in plasma. Carbon dioxide enters red blood cells and is rapidly converted there, but also within plasma, to HCO$_3^-$ and H$^+$. Equilibration between the two compartments is no longer rate limited by the slow CO$_2$ hydration reaction in plasma. The pH of the blood leaving the capillary can be expected to be constant and in equilibrium. However, as is shown in section ivD2, in the presence of lactic acid production in the tissue, this must not necessarily be so. At the end of capillary transit, it may even be possible that H$^+$ concentration in plasma is too high compared with intraerythrocytic concentration for equilibrium to be established across the erythrocytic wall, since equilibration of lactic acid across this wall is a slow process.

For CO$_2$ excretion, it is essential that there is a rapid chemical reaction of CO$_2$. However, how and how fast acid-base equilibrium is established in the blood depends on the sites of CA localization and its activity. This and the velocity of other CO$_2$ reactions will therefore be considered in the following sections.

E. Interconversion Between CO$_2$ and HCO$_3^-$

The interconversion between CO$_2$ and HCO$_3^-$ without a catalyst is rather slow and may require more than 1 min to approach completion, a time much too long compared with the capillary transit time, which is ~1 s. Carbon dioxide hydration/dehydration reactions are accelerated between 13- and 25,000-fold by intraerythrocytic CA activities (46, 47). With such a CA activity, the interconversion between CO$_2$ and HCO$_3^-$ inside erythrocytes requires only 2 ms for 95% completion.

The participants of this reaction, HCO$_3^-$ and, in particular, the H$^+$ (see sects. mC I, mD, and iv) are involved in other reactions, so the time course of their concentration is also dependent on the kinetics of other reactions. For a complete understanding of the overall time course of CO$_2$ exchange, these reactions have also to be considered.

1. Catalysis by CA in blood

Carbonic anhydrase is found in the blood of all vertebrates. With respect to location, isozyme types, and coexpression of the anion exchanger (capnophorin), there are very interesting variations between different species from the lower vertebrates to mammals (Table 4) that may shed light on the increasing efficiency of CO$_2$ excretion in the course of evolution.

A) Cytoplasm of erythrocytes. Carbonic anhydrase was first detected by Meldrum and Roughton (118) [for review, see Maren (113) and Klocke (105)]. Briefly, isozyme CA I with a relatively low specific activity occurs in the red blood cells of all vertebrate groups with the exception of the cat family and a few other species; it is absent in the red blood cells of the cat, lion, jaguar, tiger, leopard, ox, chicken, and frog (18, 115). In primitive agnathans (lamprey, hagfish) and elasmobranchs (dogfish), CA I is the only isozyme present (114). It is somewhat less inhibitable by sulfonamides and considerably more susceptible to anions than CA II. Isozyme CA II with a specific activity that is ~10 times higher than that of CA I is probably the most widespread form and occurs in the red blood cells of all vertebrates except agnathans and elasmobranchs.

A mechanism for rapid HCO$_3^-$/Cl$^-$ exchange across the erythrocyte membrane is present in almost all vertebrate red blood cells and is missing only in the most primitive vertebrate group, the agnathans (lamprey, hagfish; Refs. 39, 131, 171, 172). The consequence of this has been discussed by Nikinmaa (126). In these fish this prevents the utilization of plasma HCO$_3^-$ in CO$_2$ excretion on a physiological time scale. Together with the rather flat CO$_2$ binding curve, CO$_2$ transport in these animals appears rather inefficient, yet in the lamprey, CO$_2$ transport potential is as great as in the highly active teleosts despite the missing anion exchanger. In this species, the disadvantage is overcome by a high intraerythrocytic pH, resulting in a high intracellular binding capacity for CO$_2$ and a marked Haldane effect. However, the intracellular buffering capacity is separated from the plasma compartment in lampreys due to the low membrane permeability to HCO$_3^-$. As a consequence, extracellular metabolic acid loads cause marked fluctuations in plasma pH. Thus the major advantage gained by the rapid anion exchanger appears to consist of an improved effective extracellular buffering (with access to the intracellular buffering power) rather than in a major improvement of gas transport (126).

The acceleration of the hydration-dehydration velocity by CA within erythrocytes is considerable. An activity (factor by which the rate of CO$_2$ hydration is accelerated) of 13–14,000 was reported by Forster and Itada (46), and
figures of 23,000 and 25,000 have been obtained by Wistrand (184) and by Forster et al. (47). The cytosolic CA enzymes may be not uniformly distributed within the red blood cells. Some indications have been proposed to suggest that their concentration may be increased near the cellular border. Interactions of CA are reported with the plasmalemmal anion exchanger (capnophorin = band 3; Ref. 98), and it would seem a most efficient place to catalyze $\text{CO}_2 - \text{HCO}_3^-$ hydration-dehydration reaction in close neighborhood to $\text{HCO}_3^-$/$\text{Cl}^-$ exchange. Parkes and Coleman (133) reported an enhancement of CA activity by erythrocytic membranes; CA II and CA I activity were increased 3.5- and 1.6-fold, respectively, by the presence of red cell membranes. Whether in their erythrocytic membrane preparation the effective structure was the band 3 protein can only be speculated. Although these observations have not been confirmed yet by other investigators, there are several studies of the problem whether part of red cell CA is firmly bound to the erythrocyte membrane. Whereas Enns (40) had found CA in red cell ghosts, later studies by Tappan (170), Rosenberg and Guidotti (145), and Randall and Maren (139) came to the conclusion that red cell CA is a truly cytosolic enzyme and not membrane bound.

b) Plasma. No CA activity aside from that attributable to lysed erythrocytes was ever found in plasma, with the sole exception of dogfish (Scyliorhinus canicula; Ref. 186). Also, there is no CA activity on the outside surface of erythrocytes or available to plasma, as was confirmed by Effros et al. (37).

However, in tissues where especially large amounts of $\text{CO}_2$ leave or enter the blood, there is extracellular catalysis available to the capillary plasma in some species. This is achieved by an extracellular CA bound to membranes, the membrane-bound isozyme CA IV, which provides catalytic activity to the plasma. Such a membrane-bound CA was found in the lung (36, 104, 150) and gill (28). In skeletal muscle, the first evidence for the presence of such a CA in dog, cat, and rabbit was provided by measurements of the distribution space of labeled $\text{HCO}_3^-$ (37, 50, 51, 189) and by measurements of the postcapillary pH kinetics (128).

With the histochemical method of Hanson, staining of endothelial membranes as well as sarclemma was observed in skeletal muscle (140, 141). Immunohistochemical studies employing anti-CA IV antibodies at the light microscopic level revealed staining of capillary walls, which would indicate that CA IV is associated with endothelial cell membranes (157). With the use of semithin sections and a more sensitive immunocytochemical technique, however, capillaries and sarclemma were found to be stained, and in antibody-treated ultrathin sections of skeletal muscle studied by electron microscopy, membrane-bound CA IV was found to be associated with capillary endothelium, sarclemma, and sarcoplasmic reticulum (SR) (24). That sarcomemmal and SR CA IV were visible in ultrathin sections but not in cryosections was attributed to a poor accessibility of CA IV at these locations in the 7-$\mu$m-thick untreated cryosections. Another approach has been used by Geers et al. (51). Measuring the space of distribution of labeled $\text{HCO}_3^-$ and its reduction by CA inhibitors, Geers et al. (51) observed that the effectiveness of macromolecular CA inhibitors of different molecular size (Prontosil-dextran of mol wt 5,000 vs. 100,000) indicates the presence of CA in the interstitial space. Indirect although strong evidence for this CA to be associated with the sarclemma was obtained by intracellular and cell surface pH microelectrode measurements on skeletal muscle fibers by deHemptinne et al. (25). They observed a transient alkaline pH shift on the surface of these fibers upon exposure to propionate, whose magnitude was greatly increased in the presence of the CA inhibitor acetazolamide in the extracellular space. This was interpreted to show that in the presence of extracellular sarcomemnal CA $\text{CO}_2 - \text{HCO}_3^-$ acts as a rapid and efficient source of $\text{H}^+$ that enter the cells together with the propionate ion. Analysis of isolated sarcomemnal vesicles demonstrated the presence of high activities of CA associated with the sarclemma (179), and it was shown by Western blotting with anti-CA IV antibody that this sarcomemnal CA is isozyme CA IV (175). In conclusion then, the present state of evidence indicates that in skeletal muscle, membrane-bound CA IV is associated with endothelial as well as with sarcomemnal membranes, in addition to a CA bound to the sarcoplasmic reticulum membrane.

In the case of lung tissue, it was estimated by Bidani et al. (11) that the CA of rat pulmonary vasculature catalyzes the extracellular hydration-dehydration reaction by a factor of 130–150, a figure that may appear rather small compared with the intraerythrocytic activity of >10,000. However, the calculations described below indicate that an activity of 100 in the plasma within the capillary bed of skeletal muscle should be sufficient physiologically (see sect. nD2). No estimates of intracapillary CA activity in muscle capillaries are available.

The localization pattern of CA in blood is further complicated by the presence of a CA inhibitor in the plasma of some species, which ensures the absence of any activity of soluble CA in plasma. This was first described for dog and fish (14) and later for pig, sheep, rabbit, and various fish species (74, 75, 77, 83, 109, 137, 149). The molecular size of this endogenous CA inhibitor was determined to be 10–30 kDa for the eel (74) and 79 kDa for the pig (148).

In view of the presence of an extracellular membrane-bound CA activity available to plasma in lung and muscle, the existence of a plasma CA inhibitor seems astonishing. However, some experiments indicate that the plasma inhibitor inhibits erythrocytic cytosolic CA rather...
well, but CA from lung tissue homogenate (membrane-bound CA; dog) only incompletely (83). Similarly, plasma inhibitor from pigs showed a less than complete inhibition of vascular CA activity in lungs of rats (78), where the vascular activity of CA is known to be CA IV located on the extracellular luminal surface of capillary endothelial cells.

It may be hypothesized that, due to its molecular size, the plasma inhibitor has no access to the interstitial space. Thus a CA associated with the sarcolemma may be left uninhibited by the plasma inhibitor, because a macromolecule of this size may not enter the interstitial space to a great extent. Even the endothelial membrane-bound CA IV in the lung appears to be only partly inhibited, and this should also be true for capillary CA IV of muscle (and, for example, of the brain).

We conclude that the plasma inhibitor will inhibit erythrocytic CA released from any hemolyzed red blood cells throughout the blood vessels rather completely, thus reducing the dehydration/hydration reaction in the plasma to the uncatalyzed velocity, whereas in vascular regions with a membrane-bound CA, e.g., muscle, heart, lungs, and others, a marked catalysis of the dehydration/hydration reaction can take place even in the presence of a plasma inhibitor. Thus CA activity available to plasma appears to be confined to precise localizations within the circulation that are equipped with a capillary CA.

The effect of presence of CA in the plasma has been studied by Wood and Munger (186) for the rainbow trout. They found that CA attenuated postexercise increases in PCO2 and decreases in arterial pH by producing an increase in CO2 excretion during exercise. However, the normal postexercise hyperventilation was also greatly attenuated when CA was present in the plasma, as was the normal increase in the plasma levels of epinephrine and norepinephrine. They concluded that CO2 is an important secondary drive to ventilation in fish, and by increasing CO2 excretion by the presence of CA in the plasma this drive is diminished. The plasma CA inhibitor will ensure that no CA activity of hemolyzed erythrocytes is present and thus will contribute to maintain a high level of ventilation in certain situations, which will be favorable for O2 supply.

E. Interconversion Between CO2 and Carbamate

The kinetics of oxylabile carbamate was thoroughly reviewed by Klocke (105). We only briefly summarize the relevant facts in these sections.

1. In plasma

The kinetics of this interconversion do not seem to be important for overall CO2 kinetics, since venous and arterial plasma carbamate concentrations are almost identical. The kinetics of plasma carbamate formation were characterized by Gros et al. (61) by a half-time of this reaction of 0.047 s.

2. In erythrocytes

The binding of CO2 to hemoglobin in solution has long been known to be quite rapid, requiring a time to reach completion of 0.1–0.2 s (44), which corresponds to a half-time of ~0.04 s. Gros et al. (68) have studied the kinetics of hemoglobin carbamate formation in a wide range of pH and PCO2 values using a pH stopped-flow technique. They determined kinetic constants for the forward reaction of amino groups and CO2, kν, for the α-chain and the β-chain α-NH2 groups in addition to the ε-NH2 groups of human oxy- and deoxyhemoglobin. Table 5 shows the complete set of constants reported by Gros et al. (68) with kν, pKν, and pKν, which describe their kinetic measurements. With these constants, overall carbamate kinetics under physiological conditions of pH and PCO2 were estimated to possess a half-time of 200 ms and to require ~1 s to reach equilibrium by 95%. Their measurements were performed in the absence of 2,3-DPG, and these times may become slightly shorter when 2,3-DPG is present. Nevertheless, their estimate of the half-time of carbamate formation is considerably greater than that of Forster et al. (44) but is similar to Klocke’s estimate (102) of the half-time of mobilization of oxylabile carbamate of 0.12 s, which was obtained in the presence of 2,3-DPG.

### III. CARBON DIOXIDE TRANSPORT IN MUSCLE

#### A. CO2 Production in Muscle

Unlike most other tissues, muscle exhibits a vast range of aerobic (and anaerobic) metabolic rates. In humans, O2 consumption of muscle tissue can rise 15–20-fold from resting values of ~10 μmol·min⁻¹·100 g⁻¹, and even higher increases have been reported from 6.3

| Table 5. Velocity constants, kν, and equilibrium constants for carbamate reactions of human hemoglobin |
|-------------------------------------------------|--------|--------|--------|
| a-NH2 M⁻¹·s⁻¹ | a-NH2 M⁻¹·s⁻¹ | a-NH2 M⁻¹·s⁻¹ |
| Oxyhemoglobin kν | 660 | 430 | 14,600 |
| pKν,oxy | 6.72 | 6.42 | 10.45 |
| pKν,oxy | 5.58 | 5.00 | 5.07 |
| Deoxyhemoglobin kν | 4,320 | 1,040 | 8,800 |
| pKν,deoxy | 7.32 | 6.35 | 10.45 |
| pKν,deoxy | 5.04 | 4.39 | 5.09 |
| Number of amino groups | 2 | 2 | 44 |

Experimental conditions are as follows: 37°C, 0.15 M NaCl, absence of 2,3-DPG (68, 69).
Malian species have vastly different maximal specific O$_2$ kPa (100 mmHg) during exercise (for example, Ref. 95). The P$_{co2}$ values in the venous blood leaving the skeletal muscle have also been measured and are ~5.32–5.99 kPa (40–45 mmHg) at rest and can rise to as much as ~13.3 kPa (100 mmHg) during exercise (for example, Ref. 95).

Although different muscle types and different mammalian species have vastly different maximal specific O$_2$ consumption rates, maximal specific mitochondrial O$_2$ consumption differs considerably less. At maximum O$_2$ consumption (V$_{O2}$max), mitochondria of different species consumed 4.56 ± 0.61 ml O$_2$-min$^{-1}$·ml$^{-1}$ (87). This indicates that it is essentially mitochondrial density in muscle fibers that determines maximal specific O$_2$ consumption of these fibers.

Carbon dioxide produced within muscle mitochondria has to diffuse through the intracellular compartment and cross the sarcolemmal membrane and the capillary wall to reach the convective medium blood. Because all the membranes crossed by CO$_2$ along this diffusion pathway are considered highly permeable to CO$_2$, their surface area is of no relevance for CO$_2$ transport, but this area may be important for the permeation of ions associated with gaseous exchange. Among these membrane barriers, the capillary wall has by far the smallest surface area, only ~1/5 of the entire area of the sarcolemma (185) and only ~1/200 of the total area of the inner mitochondrial membranes (87). The following fluxes of respiratory gases occur across the surface of the capillary wall. Maximal flow of O$_2$ per area of capillary wall is 1.3–1.9 µl O$_2$-min$^{-1}$·cm$^{-2}$ as calculated from Conley et al. (20), where the higher values have been measured in more athletic species (dog, pony) and the lower values in less athletic ones (goat, calf). Corresponding maximal total CO$_2$ flux across capillary wall can be expected to be ~15% lower than the respective O$_2$ fluxes (~60 nmol CO$_2$-min$^{-1}$·cm$^{-2}$). The area of inner mitochondrial membranes being larger, CO$_2$ flux across this membrane is expected to be ~60 nmol CO$_2$-min$^{-1}$·cm$^{-2}$. This may indicate that the capillary wall could be a significant barrier to ion fluxes associated with CO$_2$ transport.

B. Localization of CA in Skeletal Muscle

As discussed for erythrocytes, dissolved CO$_2$ gas with few exceptions is highly permeable across biological membranes, but the more abundant species, HCO$_3^-$, is not. This permeability difference requires conversion of HCO$_3^-$ to CO$_2$ at a sufficient speed in red blood cells as well as in muscle cells before permeation of the membrane occurs, and only CA can ensure this rapid conversion.

Several types of CA are present in various parts of skeletal muscle as has been reviewed by Gros and Dogson (60) and recently by Henry (79). Table 6 gives a summary of CA localizations in skeletal muscle.

1. Capillary endothelium

As discussed in section II, there is clear evidence that skeletal muscle capillaries possess an endothelial membrane-bound CA. The evidence that this enzyme is CA IV appears convincing.

2. Sarcolemma

Carbonic anhydrase associated with this membrane was found with a variety of methods. The first evidence for the presence of an extracellular catalysis of the hydration/dehydration reaction in the capillary bed of skeletal muscle arose from functional studies. From observation of the distribution space of H$^{14}$CO$_3^-$ and its reduction in the presence of CA inhibitors, it was concluded that an extracellular CA in mammalian skeletal muscle exists (38). Its inhibition properties were different from those of the cytosolic enzymes, and it was concluded that this isozyme is present in the interstitial space and probably bound to the sarcolemma (50, 51). Other functional stud-

<table>
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<th>Localization</th>
<th>CA</th>
<th>Fiber Type</th>
<th>Species</th>
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<tr>
<td>Capillary endothelium</td>
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<td>157</td>
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<td>Capillary wall</td>
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<td>Sarcolemma</td>
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<td>Cytosol</td>
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<td></td>
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<tr>
<td>Mitochondria</td>
<td>CA V</td>
<td>All</td>
<td>Present in guinea pig</td>
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<td></td>
<td></td>
<td></td>
<td>Absent in rabbit, rat, and mouse</td>
<td>17, 124</td>
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CA, carbonic anhydrase.
ies have indicated that an extracellular CA available to plasma is involved in fast pH equilibration of the venous effluent and the interstitial space. With the use of a stop-flow technique, it was shown that an electrolyte perfusate had access to a CA while it passed through the hindlimb capillary bed. By inhibiting this extracellular CA, a pH disequilibrium developed in the venous saline perfusate, and the pH of the effluent slowly became more acidic after the saline had left the capillary bed, i.e., a so-called postcapillary acid pH shift developed (129). It appears likely now that these effects, at least partly, are due to capillary endothelial CA IV.

Transient changes of surface pH, induced by sudden addition and withdrawal of propionic acid, were magnified when CA was inhibited in isolated soleus muscle from mouse and rat and in cardiac muscle from sheep, rabbit, and cat (25). Transient changes of surface pH induced by a sudden increase and decrease of $\text{PCO}_2$ were blocked by CA inhibitors in a nonvertebrate muscle, the crayfish muscle (151). In the former case, surface pH change is due to a net movement of $\text{H}^+$ across the membrane together with propionate. When sarcosomal CA is blocked, the efficacy of the $\text{CO}_2/\text{HCO}_3^−$ buffer is diminished, producing an increased pH transient. In the latter experiment, inhibition of the sarcosomal CA activity leads to a suppression of surface pH transients that are caused by net fluxes of $\text{CO}_2$, which go along with rapid changes in surface $\text{PCO}_2$ that are followed by $\text{H}^+$ production or consumption when CA is present on the cell surface, but are not (or very slowly) when CA is inhibited. These effects are clearly due to a CA bound to the external surface of muscle fibers.

In sarcosomal vesicles, a CA was found in preparations from red and from white muscles of the rabbit. The inhibition constants ($K_i$) of this sarcosomal CA toward acetazolamide, chlorzolamide, and cyanate were shown to be different from those of CA II or CA III (179). With CA IV antibodies this sarcosomal CA was identified to be CA IV (175). In semithin and ultrathin sections of rat soleus muscle, CA IV was found immunocytochemically to be associated with the sarcotubules in addition to its association with the capillary endothelium and the SR (24). In mammalian heart, CA IV was also found to be associated with the sarcotubules in addition to the capillaries (156). Thus the present state of information indicates that sarcosomal CA is the membrane-bound, glycosyl-phosphatidylinositol (GPI)-anchored isozyme CA IV.

3. **Cytoplasm**

It is well known that the sulfonamide-resistant isozyme CA III is present in high concentration in the cytoplasm of mammalian skeletal muscle type I (slow-oxidative fibers) (review, Ref. 60). A sulfonamide-sensitive CA, probably CA II, was found in the cytosol of white muscles of the rabbit (161) and in the mouse soleus (21). In the latter case, however, no measurements of the erythrocytic contamination of the muscle homogenates were done; thus CA II of erythrocytes could be present in these experiments. In contrast, in the former case, red cell contamination was carefully controlled. In the cytoplasm of white as well as red hindlimb muscles of the rat, no sulfonamide-sensitive CA was present (54). For other animal groups, studies are scarce; from functional studies, the presence of a CA in the cytosol of crayfish muscle was deduced (151), and there is one report indicating that frog white muscle has a CA II-type isozyme (155).

Mammalian heart muscle appears to contain no cytosolic enzyme but high activities of the membrane-bound form (17, 54).

4. **SR**

A membrane-bound CA was detected in preparations of SR vesicles from red as well as white skeletal muscle of the rabbit (17). This finding was confirmed by histochemical results employing the fluorescent CA inhibitor dansylsulfonamide for CA staining (17, 26). Although it has not been possible to visualize SR-CA immunocytochemically at the light microscopic level (157), membrane-bound CA IV was found to be associated with SR by electron microscopy and use of CA IV antibodies (24). This latter finding corresponds with a reaction of SR membranes with anti-CA IV in Western blots (175). Wetzel and Gros (180) have found that nevertheless the inhibitory properties of the CA of SR toward sulfonamides are significantly different from those of the CA of the sarcolemma, which may indicate either that SR-CA is an isoform somewhat different from CA IV or has different properties because of a different membrane environment. In the mammalian heart, immunocytochemical evidence at the electron microscopic level indicates that CA IV is also associated with the SR (156).

5. **Mitochondria**

Mitochondrial CA, CA V, is present in high activities in liver and kidney mitochondria (see review, Ref. 60). In skeletal muscle, mitochondrial CA was found only in muscles of the guinea pig but was not detectable in skeletal muscles of the rabbit or the rat or the mouse (Table 6). Carbonic anhydrase V has been detected in immunocytochemical studies in the mitochondria of rat skeletal muscle in addition to those in several other rat tissues (174). However, these results were dependent on an antibody that misidentified another antigen in rat mitochondria as CA V. Ohliger et al. (130) reported that malate dehydrogenase copurified with rat CA V on the inhibitor affinity column used to purify rat liver CA V for the production of the antibody. Thus the antibody used may have recognized malate dehydrogenase rather than CA V.
Thus it appears that CA V is absent in skeletal muscle mitochondria of several species.

From experiments with mitochondria of mammalian liver, it is known that mitochondrial CA V rapidly provides HCO$_3^-$ for reactions in ureagenesis and in gluconeogenesis (31, 32). Whereas the former is not known to occur in muscle, gluconeogenesis does occur to some extent in this tissue. When intact hepatocytes were incubated under conditions in which gluconeogenesis begins with HCO$_3^-$ fixation via pyruvate carboxylase (high lactate/pyruvate concentrations), treatment with CA inhibitors decreased glucose synthesis (31). Such a role for mitochondrial CA V was found in rat kidneys as well (33).

Balboni and Lehninger (5) compared CO$_2$ uptake by rat liver mitochondria, which possess CA, with heart mitochondria, which do not (34). In the liver a rapid net uptake of CO$_2$ was found in association with K$^+$ or Ca$^{2+}$ entry. It was concluded that by rapid hydration inside mitochondria H$^+$ were provided to act as counterion for these cations. In the heart, no net uptake of CO$_2$ was found using the same experimental conditions, and it was concluded that CA is not present in mitochondria of rat heart.

In contrast to these findings, Nagao et al. (124) found CA V in the mitochondria of heart muscle in rat but not in mouse. Their finding is based on CA V-specific antibodies obtained by immunizing rabbits against the COOH-terminal peptides predicted from the mouse and rat CA V cDNA.

C. Transport in the Intracellular Compartment

1. CO$_2$ elimination and facilitated diffusion

Diffusion of CO$_2$ in the intracellular compartment includes diffusion of dissolved and bound CO$_2$, as has been discussed for erythrocytes.

Diffusion coefficients of dissolved CO$_2$ measured within intact muscle cells in the sarcoplasm are not available, but for a number of small molecules and ions such as potassium, sodium, sulfate, and sucrose, it has been shown that the diffusion coefficients in the sarcoplasm were reduced by a factor of 2 compared with those in aqueous solutions (107). This would predict a CO$_2$ diffusion coefficient in the sarcoplasm of ~8 × 10$^{-6}$ cm$^2$/s at 22°C and ~1.3 × 10$^{-6}$ cm$^2$/s at 37°C. Such a value would roughly agree with what is predicted by the relation between CO$_2$ diffusion constant and protein concentration given in Figure 2.

Carbon dioxide diffusion was, however, measured across layers of intact skeletal muscle tissue including sarcolemmal membranes, and in these experiments, the diffusivity of dissolved CO$_2$ and the contribution of facilitated diffusion to overall CO$_2$ transport was estimated.

From the data of Kawashiro and Scheid (97), a diffusion coefficient $D$ of $1.19 \times 10^{-5}$ cm$^2$/s ($K = 2.93 \times 10^{-4}$ cm$^2$min$^{-1}$atm$^{-1}$) at 37°C can be derived for plain diffusion of dissolved CO$_2$ in rat abdominal muscle. When facilitated diffusion was present in their experiments, i.e., in the lower range of CO$_2$ partial pressures, the diffusion coefficient was increased by a factor of >2. Similar facilitation factors were reported for rat abdominal muscle at 25°C (60). When facilitation was suppressed by inhibition of CA, a diffusion constant $K$ of $3.8 \times 10^{-4}$ cm$^2$min$^{-1}$atm$^{-1}$ was measured, and this value increased to $6.5 \times 10^{-4}$ cm$^2$min$^{-1}$atm$^{-1}$ in the absence of the CA inhibitor. Similar contributions of facilitated diffusion were measured for other skeletal muscle types by Romanowski et al. (143). Table 7 shows their data in which the ratio $Q$ of CO$_2$ diffusion constant over acetylene diffusion constant, which is 0.9 for diffusion of the dissolved gases only, has been determined for muscle sections from heart, soleus, extensor digitorum longus, masseter, and gracilis muscles of the rabbit and for abdominal muscle of the rat. In all these muscles, the ratio $Q$ is greater than 0.9, indicating that a facilitation of CO$_2$ diffusion increases intracellular CO$_2$ transport between 2- and 3.7-fold. Thus it appears well established that at normal intracellular pH values, intracellular CO$_2$ transport is significantly accelerated by facilitated CO$_2$ diffusion. The requirement of CA in the intracellular space for this process is evident from the inhibitory effect of acetazolamide on facilitation in all muscles studied (Table 7). Because facilitation occurs even in heart muscle, which has no cytosolic CA, it appears that part of the necessary catalysis is mediated by intracellular membrane-bound CA as discussed above (e.g., SR CA). This shows that the intracellular presence of CA in muscle is useful for CO$_2$ elimination from the muscle cell, which is in contrast to Roughton’s (146) remark that in a tissue such as muscle “carbonic anhydrase is an enemy to the organism rather than a friend.”

<table>
<thead>
<tr>
<th>Muscle</th>
<th>Q, cm$^2$·min$^{-1}$·atm$^{-1}$</th>
<th>Facilitation Factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heart</td>
<td>2.4 ± 0.4</td>
<td>0.9 ± 0.2</td>
</tr>
<tr>
<td>Soleus</td>
<td>3.1 ± 0.4</td>
<td>0.9 ± 0.2</td>
</tr>
<tr>
<td>EDL</td>
<td>1.9 ± 0.3</td>
<td>0.9 ± 0.1</td>
</tr>
<tr>
<td>Masseter</td>
<td>1.9 ± 0.3</td>
<td>0.9 ± 0.1</td>
</tr>
<tr>
<td>Gracilis</td>
<td>2.9 ± 0.6</td>
<td>1.5 ± 0.1</td>
</tr>
<tr>
<td>Abdominal</td>
<td>3.4 ± 0.3</td>
<td>1.1 ± 0.1</td>
</tr>
</tbody>
</table>

Table 7. Facilitated diffusion in muscles

Quotients ($Q$) of diffusion constants $K_{CO_2}$ over $K_{acetylene}$ for various muscles from the rabbit or rat (*). Control, after 45-min preincubation in Ringer solution, pH 7.4; pH 4, after preincubation in isotonic sodium lactate of pH 4.0, acetazolamide, after preincubation in Ringer solution, pH 7.4, with $1 \times 10^{-4}$ to $6 \times 10^{-4}$ M acetazolamide. Facilitation factor is $Q$ (control)/$Q$(pH 4) and represents a factor by which CO$_2$ transport is accelerated due to facilitation. EDL, extensor digitorum longus muscle. [Data from Romanowski et al. (143).]
because it would rapidly convert the membrane-permeable CO₂ into the impermeable HCO₃⁻ and thus impair CO₂ elimination.

Facilitated diffusion is based on diffusion of HCO₃⁻ and H⁺/buffered H⁺, respectively, occurring in parallel to diffusion of free CO₂. The potential contribution of facilitated diffusion to overall diffusion depends on the ratio of HCO₃⁻ to dissolved CO₂ and, thus, depends on the actual pH in muscle cytoplasm (in addition to dependence on the concentration of mobile buffers and the presence of CA activity). In heavily exercising muscle, in addition to CO₂, lactic acid is produced and the additional H⁺ shift the equilibrium of the hydration/dehydration reaction toward CO₂ and have to be buffered and eliminated from the cell. Intracellular pH of skeletal muscle can become very low and can decrease from ~7.2 at rest to a value as low as 6.6–6.7 (6, 110) or to even lower values of 6.2–6.4 (119, 152, 183) during maximal exercise. Accordingly, during maximal work, HCO₃⁻ concentration is only two times that of dissolved CO₂, whereas during rest, the ratio of HCO₃⁻/CO₂ is ~13. As a result, less facilitation of CO₂ diffusion can be expected to take place during heavy exercise. At the same time, the “CO₂ store” in the muscle, HCO₃⁻, will be mobilized by the intracellular metabolic acidosis producing high PCO₂ values in muscle tissue and in the venous blood leaving the exercising muscle.

2. H⁺, lactic acid, and lactate diffusion

The substantial facilitation of CO₂ diffusion in muscle as seen in Table 7 implies that the muscle cell possesses a highly effective mechanism of intracellular H⁺ transport by diffusion of mobile buffers. As judged from the facilitation factors given in Table 7, this H⁺ transport mechanism is at least two times more efficient than the 66 mM phosphate buffer at pH 7 as used in Figure 3. Although there are no data on intracellular lactate diffusivity, it is expected that lactate has a diffusion coefficient similar to that estimated above for HCO₃⁻. This has the following implication. The intracellular H⁺ transport capacity, which suffices to transport H⁺ at a rate equal to the rate of HCO₃⁻ transport as it results from a HCO₃⁻ concentration difference in the millimolar range (facilitated CO₂ diffusion), will also suffice to transport H⁺ at a rate equaling the lactate flux that results from a lactate concentration difference in the millimolar range (lactic acid transport). Thus lactic acid, which is almost completely dissociated at physiological pH values, can be efficiently transported through the cell interior utilizing this facilitated H⁺ transport system. It may be noted that this H⁺ transport system under conditions of exclusively aerobic metabolism is used by the cell to maintain a facilitation of CO₂ diffusion, whereas under conditions of dominating anaerobic glycolysis and low intracellular pH, it is mainly used to transport H⁺ along with the lactate anion through the intracellular space, a prerequisite for the elimination of lactic acid from the cell.

3. CO₂ and Ca²⁺ mobilization in the SR

There is considerable evidence that H⁺, in addition to Mg²⁺ and K⁺, acts as a counteron when Ca²⁺ moves across the sarcoplasmic membrane during Ca²⁺ release and reuptake (116, 117, 164). In view of the abundance of CO₂ in the cell and its high permeability in membranes, CO₂–HCO₃⁻ seems to constitute an ideal buffer system within the SR able to produce or buffer H⁺. Without CA, the CO₂ hydration reaction has a half-time of ~10 s. This is by far too slow in view of the rapid Ca²⁺ movements across the SR membrane that have half-times of 10–100 ms. Bruns et al. (17) have postulated that the CA of the SR may act to provide a rapid source and sink for H⁺ to be exchanged for Ca²⁺ across the SR membrane as illustrated in Figure 4. Carbonic anhydrase activity associated with the SR was calculated to accelerate the reaction 500- to 1,000-fold, thereby reducing the half-time to 10–20 ms. In view of the small SR-to-cytoplasm volume ratio, they postulated that this buffering mechanism would have to be more efficient in the interior of the SR than outside. From studies with SR vesicles, it could be shown that a major part of the SR CA activity is indeed catalytically active in the interior of the SR (55; G. Gros, S. J. Dodgson, E. A. Haller, B. T. Storey, and R. E. Forster, unpublished observations). By inhibiting this CA, one would expect to interfere with the rapid H⁺ exchange and thus to slow down Ca²⁺ release and reuptake. By measuring Ca²⁺ transients in skeletal muscle fibers with the Ca²⁺ indicator fura 2, Wetzel et al. (181) showed indeed that CA inhibition slows down Ca²⁺ release as well as Ca²⁺ reuptake by the SR. Geers and Gros (52, 53) showed that, as a consequence, CA inhibition of skeletal muscles results in a prolongation of time-to-peak and of half-relaxation time during isometric contraction. This constitutes an example in skeletal muscle, where the abundant presence of CO₂ in the tissue is utilized for a process resembling H⁺ secretion in other organs.

D. Transport Across Sarcolemma

As discussed for the red cell membrane, it seems reasonable to assume that the bulk of CO₂ crosses the sarcolemmal membrane in the dissolved form. On the other hand, because HCO₃⁻/Cl⁻ exchange is known to be involved in pH regulation of muscle cells (1), HCO₃⁻ permeability constants can be expected to be higher than those for lipid bilayers, and the estimate of 2 × 10⁻⁷ cm/s given by Woodbury and Miles (188) for frog skeletal muscle appears surprisingly low (see Table 3).

Transport of bound CO₂ in the form of HCO₃⁻ across sarcolemma is closely linked with other processes in-
volved in pH regulation. Bicarbonate is in equilibrium with CO₂ and H⁺, whose concentration in turn is dependent on production of lactic acid and H⁺ removal from the cell. Figure 5 shows three transport mechanisms that are involved in pH regulation of vertebrate muscle cells and how they are linked to CO₂ excretion of the cell. The transport mechanisms were reviewed by Aickin (1), and the contribution of lactate-H⁺ cotransport to pH regulation was evaluated by Juel (94).

pH regulation has been observed by measuring the rate of recovery from intracellular acidification. With the study of the effects of the presence of either SITS/DIDS or of the virtual absence of CO₂, the contribution of HCO₃⁻/Cl⁻ exchange was assessed. Observing the effect of the presence of amiloride the contribution of Na⁺/H⁺ exchange to pH regulation could be evaluated. At rest, predominantly Na⁺/H⁺ exchange and probably to a smaller extent HCO₃⁻/Cl⁻ exchange are responsible for pH regulation (Table 8; see review in Ref. 1).

During exercise, however, when indeed huge amounts of H⁺ are produced by anaerobic glycolysis inside muscle cells making highly efficient pH regulation vital, the relative contribution of these two pH-regulating mechanisms is drastically reduced. Syme et al. (168) observed that the increase in fixed acid concentration in the cytosol of the plantaris-gastrocnemius-soleus muscle group by sciatic nerve stimulation was unchanged either by the presence of DIDS or by an additional increase in CO₂. The authors concluded from this that HCO₃⁻/Cl⁻ exchange is not important for pH regulation during this condition of heavy exercise. This seems quite compatible with the idea that during exercise lactate-H⁺ cotransport is the predominant contributor to pH regulation. Westerblad and Allen (178) found that inhibition of lactate-H⁺ transport had an effect on intracellular pH only during exercise but not during rest. That during exercise this transporter carries the major load of acid extrusion was shown by studies with sarcoplasmic vesicles by Juel (92, 94). Lactate-H⁺ cotransport has by far the highest capacity to remove H⁺ from the muscle cell, and this is even more obvious for slow oxidative fibers than for fast glycolytic ones (Table 8; Ref. 92). For zero-trans-condition in vesicles, Juel (91) found a maximum velocity value for lactate-H⁺ cotransport of 48 pmol·s⁻¹·cm⁻²·sarcomemmal surface⁻¹ at room temperature. With a Q₁₀ value of 2.2 (91), this becomes ~160 pmol·s⁻¹·cm⁻² at body temperature. This lactate-H⁺ cotransporter is strongly dependent on pH. With an acidic pH in the interstitial space, the efflux of lactic acid from the muscle cell would be slowed down. Juel (93) found a steep pH dependency, predicting that a decrease of pH by 1 unit on one side of the membrane decreases lactate flux in this direction to 20%.

Let us consider a situation of heavy exercise inside and outside the sarcolemmal membrane. In Figure 5, values are given for pH, PCO₂, HCO₃⁻, and lactate as they may be present after an intense exercise period of skeletal muscle. They were taken in this example for sarcomplasm from Bangsbo et al. (6), and values for the interstitial space were assumed to be similar to venous values. The PCO₂ is assumed to be instantaneously equilibrated across the sarcolemmal and therefore assumed to be identical in the sarcolemmal and the interstitial space. There is no “facilitated CO₂ diffusion” across the sarcolemma, i.e., HCO₃⁻ does not contribute to CO₂ excretion of the cell. The reason for this is not only the low membrane permeability for HCO₃⁻ compared with that for dissolved CO₂, but also the contribution of HCO₃⁻/Cl⁻ exchange to acid extrusion, which operates in the “wrong” direction. To be effective for pH regulation and acid extrusion, HCO₃⁻ has to enter the cell, buffer H⁺, and after conversion to CO₂ leave the cell in the form of dissolved gas. The gradient for HCO₃⁻ into the cell, especially during intense exercise, is large, because intracellular pH is much lower than extracellular pH (Fig. 5). Thus no net excretion of CO₂-HCO₃⁻ from the cell is contributed by the HCO₃⁻/
Cl$^-$ exchange. The high concentration of HCO$_3^-$ in the interstitial space in this situation is useful because it provides a high buffer capacity for H$^+$ leaving the muscle cells by lactate-H$^+$ cotransport or Na$^+$-H$^+$ countertransport. The consumption of extracellular HCO$_3^-$ in the interstitial space by lactic acid producing cells (Fig. 5) is likely to be an important mechanism allowing H$^+$ efflux from the cell to be maintained. However, for this process to be sufficiently fast, CA is probably mandatory, and the extracellular sarcolemmal CA would appear to be an ideal enzyme to make the buffer capacity of interstitial HCO$_3^-$ fully and rapidly available. Without this enzyme, interstitial pH can be expected to become much lower, and this may slow down lactate-H$^+$ cotransport (see Fig. 5). Indeed, Kowalchuk et al. (106) have observed that the postexercise increase in lactate concentration in the blood was significantly lower after treatment with acetazolamide, and Geers et al. (49) have found that inhibition of extracellular muscle CA causes a decrease of lactate release from moderately exercising isolated blood-perfused muscle.

### E. Transport Across Capillary Walls

Among all the surface areas that CO$_2$ and HCO$_3^-$ as well as H$^+$ and lactate have to cross, the capillary wall has the smallest surface with only approximately one-fifth of that constituted by sarcolemma (185). Permeability coefficients for CO$_2$ are expected not to be different from those measured for lipid bilayers or the erythrocyte membrane, but direct measurements are not available. The capillary wall is known (see review in Ref. 120) to possess water channels. For skeletal muscle capillaries it was shown that these channels have pore sizes of around ~4 nm (177). This author estimated that 60% of the hydraulic capacity of cat skeletal muscle capillaries represents a “water-only pathway.” This pathway may be one of the aquaporins, which has been shown to be present in skeletal and cardiac muscle capillaries (125). On the other hand, Michel (120) postulated that through >90% of the capillary water channels not only water is able to flow, but in addition small solutes are allowed to pass through. HCO$_3^-$, H$^+$, and lactate would be classified as such small hydrophilic solutes and then could cross this barrier not only by diffusion but also by convection. Thus capillary wall permeability for HCO$_3^-$, H$^+$, and lactate can be expected to exceed that of sarcolemma. However, no direct permeability measurements for either CO$_2$, HCO$_3^-$, H$^+$, or lactate are available for capillary walls.

Capillary wall diffusion capacity for small solutes has often been measured as permeability-surface area product (PS) for substances with molecular weights similar to lactate (mol wt 89) and HCO$_3^-$ (mol wt 61). The PS for Na$^+$ (mol wt 23) was reported to be 21 ml·min$^{-1}$·100 g$^{-1}$ for cat skeletal muscle capillaries (177). The PS for EDTA (mol wt 341) of rat skeletal muscle was 12.9 ml·min$^{-1}$·100 g$^{-1}$ (72). Assuming a capillary surface area of 7,000 cm$^2$·100 g (132), these authors calculated from this value an EDTA permeability of 3·10$^{-5}$ cm/s, and a similar value was reported by Michel (120). Using the same capillary surface area, Watson’s (177) results for Na$^+$ give a capillary Na$^+$ permeability of 5·10$^{-5}$ cm/s. With their own measurements of capillary density, Shibata and Kamiya (159) found a very much lower permeability of rabbit skeletal muscle capillaries for EDTA of only 6·10$^{-6}$ cm/s. In view of possible convection through water channels in addition to diffusion, these permeability values for Na$^+$ and EDTA are astonishingly low compared with the permeabilities of the erythrocyte membrane, which, for the anion HCO$_3^-$ for example, is one order of magnitude higher (5.6·10$^{-4}$ cm/s; Ref. 160).

### Table 8. Relative contribution of different mechanisms to pH regulation of muscle cells

<table>
<thead>
<tr>
<th>Na$^+$/H$^+$</th>
<th>HCO$_3^-$/Cl$^-$</th>
<th>Lactate/H$^+$</th>
<th>Muscle Cells</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>At rest</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>80%</td>
<td>20%</td>
<td>Mouse, soleus</td>
<td>1, 2</td>
<td></td>
</tr>
<tr>
<td>-50%</td>
<td>-50%</td>
<td>Mouse, EDL</td>
<td>70</td>
<td></td>
</tr>
<tr>
<td>80%</td>
<td>20%</td>
<td>Rat, diaphragm</td>
<td>144</td>
<td></td>
</tr>
</tbody>
</table>

**Exercise condition, lactic acidosis**

<table>
<thead>
<tr>
<th>In vivo not important</th>
<th>Rat, hindlimb muscle</th>
<th>168</th>
</tr>
</thead>
<tbody>
<tr>
<td>10%</td>
<td>17%</td>
<td>73%</td>
</tr>
<tr>
<td>12%</td>
<td>16%</td>
<td>72%</td>
</tr>
</tbody>
</table>

EDL, extensor digititorum longus muscle.
IV. KINETIC REQUIREMENTS OF THE PROCESSES INVOLVED IN ELIMINATION OF CARBON DIOXIDE AND LACTIC ACID FROM MUSCLE AND UPTAKE INTO BLOOD

Figure 6 illustrates the processes involved in CO₂ and lactic acid transfer from the cytoplasm of muscle cells to plasma and into the interior of erythrocytes, as discussed in sections I–III. What is the role of these processes for the overall kinetics of CO₂ uptake into red blood cells and lactic acid transfer into the blood? Table 9 shows the times required for 95% completion of CO₂ uptake if any one of these single processes would determine the kinetics of the overall process. Table 9 gives a rough idea of how critically each process will affect the overall time course. The theoretical model of CO₂ and lactic acid exchange presented in section IV A analyzes the role of each process quantitatively.

A. Theoretical Model of CO₂ and Lactic Acid Exchange in Muscle

To understand the complex interdependence of reactions and transport processes involved in CO₂ exchange more completely, we will use a theoretical model. An analysis of postcapillary pH equilibration and the role function of CA therein has been presented primarily for the gas exchange in the lung (10, 45, 84). The following reasons prompted us to thoroughly modify existing models for the situation in skeletal muscle instead of merely extrapolating from the lung models.

1) In skeletal muscle not only CO₂ exchange but also release of lactic acid from muscle tissue has to be considered, since this represents another disturbance of pH equilibration. Lactic acid is not considered in lung models, whereas this appears necessary for skeletal muscle.

2) With a model consisting of only two compartments (erythrocytes and plasma), as has been used in the lung models, we were not able to simulate the direction of the postcapillary pH shift measured in isolated blood-perfused rat hindlimb muscle (C. Geers, O. Bertram, and G. Gros, unpublished observations), when extracellular CA was inhibited and CO₂ and lactate were released.

3) Lactate-H⁺ cotransport takes place across the sarcolemma; this implies that H⁺ are primarily accumulated in the interstitial space and buffering of H⁺ by HCO₃⁻, the most important buffer in this compartment, will take place there. Thus catalysis of the reaction HCO₃⁻ + H⁺ ↔ CO₂ in the interstitial space to be useful for the buffering of these H⁺. Thus inclusion of interstitial space as another compartment into the model appears indispensable in the case of skeletal muscle.

4) With such a third compartment (erythrocytes/plasma/interstitial space), the functional role not only of an interstitial (sarcolemmal) CA, but also that of a CA inhibitor present in the plasma of a number of species can be studied, since the available evidence suggests that CA is present in each of the three compartments: erythrocytes (cytosolic CA), plasma (CA bound to endothelium), and interstitial space (CA associated with the sarcolemma).

The starting point of the present model was a modified, in some respects (carbamate, deoxygenation) simpler, version of the analysis of postcapillary pH equilibration as it has been described by Bidani et al. (10). We extended this model to include lactic acid exchange and the interstitial space. This model analyzes for steady-state conditions single capillary passages of blood through

<table>
<thead>
<tr>
<th>Process Limited by</th>
<th>Time (95%), ms</th>
</tr>
</thead>
<tbody>
<tr>
<td>Buffering of H⁺</td>
<td>Instantaneous</td>
</tr>
<tr>
<td>Intracellular CO₂ diffusion</td>
<td>6</td>
</tr>
<tr>
<td>CO₂ permeation of red cell membrane</td>
<td>6</td>
</tr>
<tr>
<td>Diffusion of CO₂ from muscle to plasma</td>
<td>?</td>
</tr>
<tr>
<td>Velocity of intraerythrocytic CO₂ hydration</td>
<td>2</td>
</tr>
<tr>
<td>(14,000 fold accelerated, A = 14,000)</td>
<td></td>
</tr>
<tr>
<td>HCO₃⁻/Cl⁻ exchange (82)</td>
<td>430–500</td>
</tr>
<tr>
<td>Carbamate reaction (82, 102)</td>
<td>500</td>
</tr>
<tr>
<td>Permeation of lactate or HCO₃⁻ through capillary wall (with assumed permeability of 0.0002 cm/s)</td>
<td>1,000</td>
</tr>
<tr>
<td>Extracellular CO₂ hydration in plasma Without CA activity [t₁/₂, 8 s; (57)]</td>
<td>34,000</td>
</tr>
<tr>
<td>100-fold accelerated (A = 100)</td>
<td>340</td>
</tr>
<tr>
<td>Uptake of lactic acid in red blood cells [t₁/₂,effluent, 35 s; (91)]</td>
<td>150,000</td>
</tr>
</tbody>
</table>

Where included, reference numbers are given in parentheses. t₁/₂, half-time.
muscle tissue and describes the intra- and postcapillary changes of pH, CO$_2$, HCO$_3^-$, and lactate in erythrocytes, plasma, and the interstitial space. As an estimate for lactate and CO$_2$ excretion for a given steady-state condition, muscular arteriovenous concentration differences of lactate and CO$_2$ were calculated. This model does not describe time-dependent changes in muscle cells or changes in lactate and CO$_2$ production rates during the onset of exercise.

B. Reactions Included in the Model and Their Mathematical Form

The entire skeletal muscle is thought of as a single unit consisting of muscle cell interior, interstitial space, plasma, and erythrocytes. These compartments are treated as layers with diffusion taking place only perpendicular to the boundaries separating them. Interstitial, erythrocyte, and plasma volumes are given as values relative to blood or capillary volume. The available surface areas of each compartment boundary are given per blood volume and are calculated using estimates of capillary volume-to-skeletal muscle volume ratio (158), hematocrit, erythrocyte surface-to-volume ratio, and a capillary radius of 3.5 μm. Within each compartment molecules are assumed to be always homogeneously distributed. Activity of CA associated with membranes, sarcolemma, and capillary wall was assumed to be homogeneously present in the respective fluid compartment, interstitial space, and plasma. Concentrations inside skeletal muscle cells are assumed to be constant throughout one calculation, although values used are varied to simulate rest or exercise conditions. Blood flow is assumed to be constant. Values for arterial blood entering the capillary are set to standard arterial values; thus for the calculations performed here, these were assumed to be independent of the venous values (“open circuit” system).

During the capillary transit, the blood takes up CO$_2$, H$^+$, and lactate from the muscle cell via the interstitial space. Chemical and transport events that occur during gas and lactic acid exchange, which we have included in our calculations, are with few exceptions shown in Figure 6. With steady-state conditions, it is assumed that within each part of the interstitial space along the capillary wall concentrations are constant. Thus the sum of influx and efflux into this compartment and the rate of change of chemical reaction has to be zero for CO$_2$, HCO$_3^-$, H$^+$, and lactate. A concentration profile is calculated for these substances parallel to the capillary. For each molecular species, equations describing its rate of change are devised for plasma and erythrocytes, and new concentrations of each substance are calculated at successive points of time, with time intervals <1 ms, as the blood travels along the capillary and until 120 s after it has left the capillary. The mass balance of each molecular species in each compartment considers the rate of consumption and production of that species by chemical reaction within its compartment and/or net transport of the species in and out of the compartment. The reactions and transport events included in the analysis are described as follows. For CO$_2$, 1) hydration/dehydration reaction catalyzed by CA or uncatalyzed; 2) diffusion between skeletal muscle cell, interstitial space, and erythrocytes; and 3) binding of CO$_2$ to hemoglobin within erythrocytes (not shown in Fig. 6). For HCO$_3^-$, hydration/dehydration reaction catalyzed by CA or not (see point 1); 4) diffusion from interstitial space into plasma, and vice versa; and 5) movement between plasma and erythrocytes via anion exchanger. For H$^+$, hydration/dehydration reaction catalyzed by CA or not (see point 1); 6) buffered by proteins inside erythrocytes and plasma (not shown in Fig. 6); 7) cotransport of H$^+$ and lactate ions across the sarcolemmal and red cell membrane; 8) release of H$^+$ by carbonate reaction (not shown in Fig. 6); 9) uptake of H$^+$ due to deoxygenation of hemoglobin (not shown in Fig. 6); and 10) diffusion across the capillary wall. For lactate, cotransport of H$^+$ and lactate ions across the sarcolemma and erythrocytes (see point 7); 11) movement of lactate ions via anion exchanger between plasma and erythrocytes.

The change of concentration for each species was calculated for interstitial space, plasma, and erythrocytes. The flux of water across the red cell membrane is calculated as described by Bidani et al. (10) using a hydraulic permeability coefficient and the difference in osmolality across the membrane. Table 10 lists the numerical values used for the computations.

C. Permeability of the Capillary Wall to Lactate

Permeability values for lactate across the capillary wall in skeletal muscle are not available. Although the capillary wall has not been considered to form a barrier of functional significance for lactate diffusion (94), one study using microdialysis has demonstrated that interstitial lactate is not always equilibrated with blood plasma lactate (112). Permeability values for muscle capillaries cited for molecules of a size roughly similar to that of lactate (mol wt 89) are 6 × 10$^{-6}$ cm/s for Cr-EDTA (mol wt 341) in rabbits (159), 3 × 10$^{-5}$ cm/s for EDTA in rats (72), and depending which capillary surface was used for the calculation 0.5–1 × 10$^{-5}$ cm/s for EDTA in cats (177) and 2–5 × 10$^{-5}$ cm/s for sodium (mol wt 23) in cats (177).

Figure 7 shows that by using these permeability values of the capillary wall for our model calculation we found it impossible to achieve arteriovenous differences for lactate as high as they have been reported to occur. Arteriovenous differences for lactate during and after a
bout of heavy exercise can be as high as 6.6 mM for human skeletal muscle, with intracellular lactate concentration rising to 28 mmol/l cell water and a venous plasma lactate concentration of 14 mM (95).

For example, for a lactate permeability of $2 \times 10^{-5}$ cm/s, only very low arteriovenous concentration differences for lactate were obtained of $\ll 1$ mM, and a prolongation of the transit time to twice the standard value of 1 s for the calculation had only a small effect. The calculated arteriovenous difference becomes only $\sim 2.2$ mM, i.e., the venous concentration rises to 4.2 mM from the generally assumed arterial concentration of 2 mM. With this permeability value, the lactate concentration across capillary wall can be calculated to be as high as $\sim 12$ mM. This would imply that the limiting barrier for lactate excretion is the capillary wall rather than the sarcolemma and would be incompatible with the experimentally obtained arteriovenous lactate concentration differences of 6 – 7 mM for heavy exercise (95).

On the basis of the calculations shown in Figure 7, it seems clearly warranted to assume a lactate permeability of the muscle capillary of at least $1 \times 10^{-4}$ cm/s. The calculations with the theoretical model reported below were therefore performed with a capillary permeability for lactate of $2 \times 10^{-4}$ cm/s. However, with an increase in permeability only the arteriovenous difference is still too low to explain experimental data; thus in addition to this higher permeability value, a longer transit time is probably present in lactate-producing muscle.

The range of muscle capillary transit times reported in the literature is rather wide. Compared with the values in the lung, they were found to be approximately twice as long in a variety of species (98). Values for minimal mean capillary transit times during maximal blood flow under exercise at maximal aerobic capacity were computed from total capillary blood volume/muscle blood flow by Kayar et al. (98) to be 0.7 – 0.8 s (dog, goat) and 0.8 – 1.0 s (horse, steers). For humans, a mean transit time of 0.8 – 0.9 s was estimated at maximal leg exercise (153).

At rest, directly measured red cell transit times across the capillary network were considerably longer, 3 – 4 s (hamster, cremaster muscle; Ref. 154). Observing erythrocyte velocity and measuring capillary length, Honig et al. (86) calculated mean transit times of 4.3 s with a range of 0.09 – 43 s in rat gracilis.

| TABLE 10. Data used in analysis of blood passing through skeletal muscle capillaries |
|---------------------------------|---------------------------------|
| Half-time of carbamate reaction (103) | 0.12 s |
| Surface area of human erythrocytes/ml blood | $\sim 7,800$ cm$^2$/cm$^3$ |
| Surface area of capillary wall in skeletal muscle/ml blood, calculated for mean capillary diameter of 7 μm [for rat measured, 8,700 cm$^2$/cm$^3$ (158)]. | $5,700$ cm$^2$/cm$^3$ |
| Surface of sarcolemma/liter blood; $\sim 5$ times capillary surface | $3 \times 10^6$ cm$^2$/cm$^3$ |
| Membrane CO$_2$ diffusion capacity (10) | 8.55 mmol CO$_2$ · 1 blood$^{-1}$ · s$^{-1}$ · Torr$^{-1}$ |
| Thickness of erythrocyte membrane | 10$^{-3}$ cm |
| CO$_2$ hydration velocity constant (147) | 0.13 s$^{-1}$ |
| H$_2$CO$_3$ dehydration velocity constant (45) | 57.5 s$^{-1}$ |
| Acid dissociation constant for H$_2$CO$_3$ (147) | 0.35 mM |
| CO$_2$-HCO$_3^-$ equilibrium constant | 7.91 $\times 10^{-4}$ mM |
| Michaelis constant for lactate-H$^+$ cotransport in skeletal muscle (91) | 23.7 mM |
| $V_{\text{max}}$ for H$^+$-lactate cotransport (37°C) | 160 pmol · cm$^{-2}$ · s$^{-1}$ |
| Factor for reduction of $V_{\text{max}}$ with pH decrease by 1 unit (93, 94) | to 20% decreased |
| Equilibrium constant for lactic acid | 10$^{-3.86}$ |
| Faraday constant | 96,480 C/mol |
| HCO$_3^-$ mobility (using $P = 5.6 \times 10^{-4}$ cm/s for red cell membrane) (160) | $2.0 \times 10^{-11}$ cm$^2$ · mV$^{-1}$ · s$^{-1}$ |
| Lactate ion mobility across red cell membrane, 10,000 less than for HCO$_3^-$ | $2.0 \times 10^{-15}$ cm$^2$ · mV$^{-1}$ · s$^{-1}$ |
| Red cell hydraulic coefficient (41) | 0.041 cm/s |
| Buffer capacity in erythrocytes | 60 mmol H$^+$/unit pH |
| Buffer capacity in plasma | 5.5 mmol H$^+$/unit pH |
| H$^+$ taken up due to hemoglobin oxygenation (101) | 0.7 mmol H$^+$/mmol Hb deoxygenated |
| H$^+$ taken up due to carbamate formation (8) | 1.8 mmol H$^+$/mmol carbamate formed |

Where included, reference numbers are given in parentheses. $V_{\text{max}}$, maximum velocity.

FIG. 7. Computed effect of capillary permeability for lactate on arteriovenous concentration difference of lactate. Conditions chosen for the calculation are as follows: intramuscular lactate concentration, 40 mM; arterial lactate concentration, 2 mM; PCO$_2$, 7.3 kPa (55 mmHg). Carbonic anhydrase (CA) activity is given as the factor by which the uncatalyzed reaction is accelerated, i.e., an activity of A = 1 indicates the uncatalyzed reaction. CA activities assumed for these calculations were as follows: in erythrocytes, A = 6,500; CA associated with capillary wall expressed as activity in capillary plasma, A = 100; sarcolemmal CA expressed as activity in the interstitial space, A = 100. Dotted line, capillary transit time 2 s; solid line, capillary transit time 1 s.
It may be noted that although the value of the capillary transit time is obviously critical for the calculated arteriovenous difference for lactate (Fig. 7), this is not the case for the arteriovenous difference for CO₂. Almost no difference was calculated for CO₂ excretion using transit times between 0.5 and 2 s when no lactate excretion was present. However, when lactate excretion was present and increased with increasing transit times, as just explained, the calculated arteriovenous difference for CO₂ decreased with increasing transit times, probably due to the accompanying metabolic acidosis. It may be speculated whether long transit times are useful (and present?) in more glycolytically working muscles such as gracilis muscle, in contrast to oxidatively operating muscles, in which shorter transit times might be sufficient.

D. Effect of CA at Different Localizations on Equilibration of Intravascular pH, CO₂ Excretion, and Excretion of Lactic Acid

1. CA inside erythrocytes

It is well established that the presence of an intr erythrocytic CA is essential for an efficient transport of CO₂ by the blood. For the calculations of Figure 8, a constant PCO₂ in muscle cells of 7.3 kPa (55 mmHg) was assumed, and it was further assumed that CA is available to plasma by a CA bound to the endothelium with a 100-fold acceleration of the hydration velocity (A = 100). In addition, it was assumed that muscle lactate concentration is low so that there is negligible lactate excretion. The calculations give the following results: 1) when only uncatalyzed dehydration-hydration reaction occurs in erythrocytes (no catalysis, defined here as CA activity A = 1), a very low arteriovenous difference for total CO₂ (i.e., CO₂ + HCO₃⁻ + carbamate) is obtained (Fig. 8, bottom). The CO₂ binding capacity of the blood at the given PCO₂ of 7.3 kPa (55 mmHg) can only partially be used, because the velocity of the hydration reaction in erythrocytes is far too slow in comparison with the capillary transit time of 1 s. Most of the arteriovenous difference under these conditions is due to dissolved CO₂ and carbamate.

2) When the dehydration-hydration reaction velocity is 1,000-fold enhanced (CA activity A = 1,000), the arteriovenous difference for CO₂ is 98% of its maximal value, which can be achieved given the conditions indicated (Fig. 8, bottom). This is close to the value of A = 600 that can be estimated from Roughton (147) to be the necessary acceleration of the dehydration reaction in the lung for CO₂ exchange to achieve 98% of its maximal value within capillary transit time during rest. It is not clear why there is so much more CA activity inside erythrocytes than is apparently necessary. An increase of the intramuscular partial pressure of CO₂ to values as high as 13.3 kPa (100 mmHg) does not require any higher CA activity inside erythrocytes. The curve of Figure 8 showing the dependency of arteriovenous difference on CA activity is shifted to higher values of arteriovenous differences but does not alter its shape. The same holds for a higher HCO₃⁻ permeability of the erythrocyte membrane: when the HCO₃⁻ permeability is assumed to be three times higher than the standard value used, the arteriovenous differences are unaltered compared with those seen in Figure 8. This implies that no additional CA would be necessary if the permeability of the erythrocyte membrane for HCO₃⁻ were higher. (It may be noted that massive reduction of HCO₃⁻ permeability per se decreases CO₂ excretion in the lung, Ref. 23). In other words, neither does the HCO₃⁻ permeability of the red cell membrane set a limit to CO₂
uptake, nor does red cell CA activity ever become limiting at increased levels of CO₂ production. A possible situation where intraerythrocytic CA may become more critical, which has to our knowledge never been investigated, is a severe lactic acidosis with low intraerythrocytic pH values. At a pH of 6.4, the activity of CA II decreases to ~30% of its value at pH 7.2 (99), and in this situation, more enzyme will be necessary to maintain the required activity.

3) The dotted line in Figure 8, bottom, shows arteriovenous differences of total CO₂ in the absence of extracellular, intravascular CA activity, whereas the solid line indicates presence of A = 100 in capillary plasma volume. Lack of intravascular CA results in a decrease in arteriovenous difference by an about constant amount. This is due to the inability of the plasma to utilize its own buffer capacity during capillary transit. The reduction in CO₂ uptake amounts to only a few percent at high red cell CA activities but is relatively more important when red cell CA activity is low or absent.

4) When only uncatalyzed dehydration-hydration reaction is present in erythrocytes, there is a large and very slow postcapillary pH shift of >0.15 pH units in the plasma in alkaline direction (Fig. 8, top, solid line). The ΔpH values given in Figure 8, top, represent the maximal deviations of endcapillary plasma pH from their equilibrium values. The large pH shifts occur, although in the calculation represented by the solid line, capillary CA activity is assumed to be available to the plasma during capillary transit (A = 100). In the absence of intraerythrocytic CA activity, no full pH equilibrium was achieved even within the period of 120 seconds considered in our calculations. In this case, the buffer capacity of the erythrocytes, which is ~10 times greater than that of plasma, can only be used slowly, since CO₂ within erythrocytes is very slowly converted to H⁺ and HCO₃⁻. The slow alkaline postcapillary pH shift seen here in the plasma is essentially caused by the slowly decreasing P CO₂ in the whole blood, which reflects the slow formation of HCO₃⁻ inside the red blood cell and thus the slow formation of the major storage form of CO₂ in the blood. Accordingly, the postcapillary pH shift disappears when intraerythrocytic CA activity increases beyond A = 1,000, as shown by the solid line.

5) When no CA is available to the plasma in the capillary (dotted line in Fig. 8, top), the curve showing the function of postcapillary pH change versus erythrocyte CA activity is of similar shape but is shifted by ~0.1 pH unit toward more acidic postcapillary pH changes. When in this situation intraerythrocytic CA activity is low, the differences between endcapillary pH and equilibrium pH, i.e., the overall postcapillary pH changes, as given on the y-axis of Figure 8, are small or even absent. However, immediately after leaving the capillary, pH of the plasma falls within a few seconds to increase slowly toward the equilibrium value thereafter. A similar observation has been made in lung models (10).

6) Lactate excretion is almost independent of the presence of CA in erythrocytes, as can be expected (see below and Fig. 11).

What would be the impact of CA-deficient erythrocytes in vivo? As it is well known and as Figure 8 demonstrates, erythrocytes without CA activity can transport far less CO₂ than red blood cells with CA activity, but such a situation does not exist among vertebrates. Even the most primitive of them, e.g., agnathans, has CA activity inside their erythrocytes (see Table 4).

There are genetic disorders and there are experiments with inhibition of CA activity that allow us to study the consequences of reduced levels of CA in red blood cells. Clinical manifestations attributed to deficiency of CA, the CA II deficiency syndrome, encompass osteoporosis, renal tubular acidosis, and cerebral calcifications as reviewed by Sly and co-workers (162, 163). However, in the erythrocytes of these patients, there is still activity of CA I present. This isozyme occurs normally in adult human erythrocytes at a greater concentration than CA II does, but because of its higher sensitivity for Cl⁻, it is inhibited to a large extent. At 37°C, it contributes ~50% of the normal activity in red blood cells (33). When in normal red blood cells the hydration reaction is accelerated by a factor of ~14,000 over the uncatalyzed rate (CA activity = 14,000), then loss of one-half of this activity (A = 7,000) cannot be expected to reduce CO₂ transport from muscle to blood even slightly (Fig. 8). The manifestations of CA II deficiency in other tissues are far more prominent clinically, and no disturbances of CO₂ elimination of the body are apparent.

There are no techniques available to perform experiments in vivo, in which erythrocytic CA activity only is inhibited, because after intravascular administration of CA inhibitors these will not only diffuse readily into the interior of erythrocytes but will always inhibit necessarily any extracellular CA activity in the lung as well as in other tissues, and will in addition penetrate into the cells of several other tissues. For example, CO₂ excretion across alveolar membrane will always be affected by such CA inhibitors. The overall effect of such systemic CA inhibition on blood gases, tissue P CO₂, and ventilation has been demonstrated in classical experiments by Roughton et al. (148), Mithoefer (121), Mithoefer and Davis (122), and Swenson and Maren (166). A few experiments are available in which it was attempted to demonstrate the role of CA in CO₂ excretion by specific tissues, by either observing tissue P CO₂ or organ arteriovenous differences. An increase in tissue P CO₂ by ~1.3 kPa (10 mmHg) during the reduction of CA activity has been observed for tissue surrounding the eye, whereas venous and arterial P CO₂ values were not significantly changed in this experiment (169). Kowalchuk et al. (106) measured a decrease in the
arteriovenous concentration differences for HCO$_3^-$ and CO$_2$ across the human forearm and thus a decrease in CO$_2$ excretion, during forearm exercise, after administration of acetazolamide. These effects are independent of the accompanying effect on CO$_2$ excretion by the lung, and these reductions in CO$_2$ excretion probably reflect mostly the inhibition of CA inside erythrocytes and only to a minor extent the inhibition of extracellular CA (see below). Differentiation between an effect due to red cell CA inhibition and one due to extra- or intracellular tissue CA inhibition at the moment is only possible from theoretical models such as are described in section IV, D2 and D3.

For the computations described in the following, CA activity within erythrocytes was always chosen to be 6,500 for technical reasons linked to the numerical procedure. Although the actual activity within erythrocytes is reported to be higher, this acceleration is more than fast enough not to become the rate-limiting step for the processes modeled. The size of necessary time intervals for the calculation would have to become much smaller with higher speed of the hydration reaction, and this would consequently slow down the speed of the calculation and, more importantly, increase the necessary precision requirements for all values.

2. CA at the capillary wall

Carbonic anhydrase associated with endothelium provides CA activity for plasma during capillary passage. Figure 9 shows the computational results for what the presence of CA in the plasma during capillary transit does to 1) arteriovenous difference of CO$_2$ and 2) the equilibration of pH in the plasma after blood has left the capillary. The calculations were done for the following conditions: intramuscular Pco$_2$ 7.3 kPa (55 mmHg), lactate concentration in the muscle cell of 4 mM, and hydration-dehydration reaction in the interstitial space uncatalyzed.

The calculations yield the following results (Fig. 9). 1). With the assumption of uncatalyzed velocity for the dehydration-hydration reaction inside capillary plasma, the arteriovenous difference as a measure of CO$_2$ excretion is ~6% less when compared with a situation when a CA activity of ~50 or more is available to the plasma (solid curve in Fig. 9, bottom). With a CA activity of only ~10 available to the plasma, about one-half of this increase in CO$_2$ excretion can be achieved. The absence of CA activity from capillary plasma can be compensated by an elevation of muscle tissue Pco$_2$ if muscle Pco$_2$ is raised only ~0.27 kPa (2 mmHg) in this example and all other parameters remain unchanged, then the arteriovenous difference even without plasma CA activity becomes as high as it is with plasma CA present. Thus presence of CA at the capillary wall and presence of CA activity within capillary plasma has minor consequences for CO$_2$ excretion from muscle tissue into the blood, and this decrease in excretion can be compensated for by a slightly higher Pco$_2$ gradient from muscle cells to arterial blood.

For a more severe respiratory acidosis, Pco$_2$ ~9.3 kPa (70 mmHg), the results are qualitatively similar, but absolute arteriovenous-differences are of course higher. However, the necessary increase in intramuscular Pco$_2$ to achieve a compensation of the decrease in arteriovenous difference when CA is not available to plasma is twice as high as in the former example. Thus the CA associated with capillary wall appears to become more important for efficient CO$_2$ excretion when the work load of the muscle increases.
In agreement with this, we made the following observation in an isolated blood-perfused rat hindlimb. When extracellular CA was inhibited by benzolamide and quaternary ammonium sulfonamide (QAS), inhibitors which are thought to be confined to the extracellular space and thus erythrocytic CA is left essentially uninhibited, no reduction of CO$_2$ excretion during rest and during moderate exercise with a fourfold increase in O$_2$ consumption could be detected (49). This is as is to be expected from these computational results.

Henry et al. (82), however, found in the isolated perfused white tail muscle of the trout that inhibition of extracellular CA by QAS, an inhibitor confined to the extracellular space, reduced CO$_2$ efflux from this muscle by ~30% and caused a significant increase in intramuscular Pco$_2$ by ~0.4 kPa (3 Torr). It may also be noted that inhibition of the membrane-associated CA IV of the isolated blood-free perfused lung reduced CO$_2$ excretion by this lung preparation significantly (76).

2) With respect to equilibration of postcapillary pH, however, CA associated with the capillary wall of skeletal muscle is important (Fig. 9, top). When no CA activity is present in plasma, there is a large pH shift in acidic direction after blood has left the capillary. The blood leaving the capillary is more alkaline than at equilibrium distribution between erythrocytes and plasma. Equilibration across erythrocytic membrane takes time, and postcapillary pH shift requires more intravascular CA activity than plasma CA for rapid pH equilibration in the postcapillary perfusate. In the blood-perfused hindlimb, inhibition of the extracellular CA produced postcapillary pH shifts in the acidic direction. When no inhibitors of CA were present, the postcapillary pH shift was not abolished, but instead an alkaline pH shift was observed (49).

3) For lactate excretion, our model predicts that capillary CA, i.e., CA in capillary plasma, has no effect whatsoever.

The dashed curves in Figure 9 show the effect of a plasma nonbicarbonate buffer capacity that is doubled from its normal value of 5.5 to 11 mM/ΔpH. As can be expected, this leads to an increase in CO$_2$ arteriovenous difference (and CO$_2$ excretion) by ~5%, and more intra- and extracellular CA activity is required to utilize this increased plasma CO$_2$ binding capacity. Similarly, the acid postcapillary pH shift requires more intravascular CA activity under this condition to fall toward zero. This again implies that more CO$_2$ has to be hydrated in the plasma to produce the pH required for equilibrium, when plasma buffer capacity is higher. In conclusion, capillary CA activity becomes more important with increasing plasma buffer capacity.

These computational results remain essentially unchanged with the assumption of the additional presence of CA activity associated with the sarcolemma, or interstitial CA activity. Carbon dioxide excretion and change of postcapillary pH are the same as without interstitial CA activity.

In conclusion, intravascular CA activity is of some relevance for CO$_2$ excretion, which depends on plasma buffer capacity, but interstitial CA does not contribute to this process and instead serves entirely another purpose, as shown section III D 3.

3. CA associated with the sarcolemma

Carbonic anhydrase associated with the sarcolemma is with its active center oriented toward the extracellular space and thus provides acceleration of the hydration-dehydration reaction on the muscle cell surface and in the interstitial space. Bicarbonate is therefore expected to be a potent and rapidly available buffer in this compartment, which possesses a very low nonbicarbonate buffer capacity. Juel (94) has shown that the external buffer capacity around sarcolemmal vesicles can affect lactate efflux.

Conditions chosen for the following computations were high concentrations in the muscle of both CO$_2$ (Pco$_2$
55 mmHg) and lactate (40 mM in the muscle cell). In addition to an intraerythrocytic CA activity of 6,500, an intracapillary CA activity of 100 was used. Computational results were as follows.

1) When no CA is present at the sarcolemma, the interstitial pH becomes rather low (Fig. 10, top, dotted line), indicating that interstitial HCO$_3^-$ does not react fast enough to buffer the H$^+$ of the lactic acid leaving the muscle cells. Only a very small acceleration of the dehydration rate within the interstitial space is sufficient to keep the interstitial pH close to 7.15. Under these conditions, a CA activity of only ~5 achieves a half-maximal effect. However, when almost no lactate is excreted by the muscle cell (arteriovenous lactate concentration difference ~0.6 mM), CA at the sarcolemma becomes rather unimportant for the pH equilibrium in the interstitial space (Fig. 10, top, solid line).

2) Plasma postcapillary pH changes were not influenced by presence or absence of sarcolemmal CA activity (data not shown); here intravascular CA activity, together with intraerythrocytic activity, alone is crucial.

3) When CA at the sarcolemmal surface is lacking, the arteriovenous difference for lactate is reduced to almost by one-half (Fig. 10, bottom, dashed line). As discussed above, this can be expected to occur as a consequence of the decrease in interstitial pH, which slows down lactic acid excretion via lactate-H$^+$ cotransport. A fivefold acceleration of the hydration-dehydration rate in the interstitial space is sufficient to produce a half-maximal increase in lactate excretion.

Experimentally, such an effect of CA on lactate excretion has been observed. In a blood-perfused rat hind-limb preparation, selective inhibition of extracellular CA reduced lactate excretion significantly (49). In these experiments, CA activity of the capillary wall as well as that associated with the sarcolemma were inhibited. From the experiments, therefore, it could not be decided which CA at which location is responsible for the reduction of lactate release. From the present theoretical model, we conclude that inhibition of the sarcolemmal CA only is responsible. This conclusion presumably holds also for the observations of Kowalchuk et al. (106), who reported a decreased lactate release into the blood under systemic treatment with acetazolamide.

Carbon dioxide release in Figure 10, bottom, dotted line, appears to be impaired with increasing activity of sarcolemmal CA, yet CO$_2$ release per se is not dependent on CA in this location. When no significant lactate excretion occurs, there is no change in CO$_2$ excretion per se. However, as the difference between solid and dotted lines in Figure 10, bottom, suggests, the arteriovenous difference for total CO$_2$ is higher when no or little lactate excretion occurs than when major lactate excretion is present. It is the increase in lactate excretion caused by an increase of sarcolemmal CA activity, which reduces total CO$_2$ excretion from the muscle, when sarcolemmal CA activity increases along the abscissa in Figure 10. The reason for this is as follows: when CA activity is present in the interstitial space, a higher rate of lactate-H$^+$ cotransport out of the muscle cell takes place. More H$^+$ arrive in the blood, and pH in plasma and in red blood cells decreases. This implies that, at a given PCO$_2$ (here 55 mmHg), the total CO$_2$ bound in the blood is reduced, because both HCO$_3^-$ and carbamate decrease with decreasing pH. Thus lactic acidosis decreases the total CO$_2$ release from muscle into blood at a given PCO$_2$. Because CO$_2$ production continues, the consequence is
a rise in tissue and venous blood $P_{CO_2}$ values. For the whole body, heavy exercise therefore is associated with rather high muscle venous $P_{CO_2}$ values and, as is well known, part of this CO$_2$ is mobilized by lactic acid from the CO$_2$ stores in muscle and blood.

The major conclusion from the results presented in Figure 10 then is that sarcolemmal CA plays an important role in the 1) maintenance of normal interstitial pH by making the interstitial HCO$_3^-$ rapidly available buffering of H$_3^+$ of fixed acids, and, linked to this, 2) facilitation of lactic acid release from the muscle cell by consuming the H$_3^+$ leaving the cell along with lactate. In contrast, sarcolemmal or interstitial CA does not appear to be involved in the exchange of CO$_2$ in skeletal muscle.

4. Lactic acid excretion and CA

The role of the three types of CA considered here for the excretion of lactic acid from muscle is summarized in Figure 11. It is immediately apparent from Figure 11 that only interstitial, sarcolemmal CA plays a major role. Lack of this enzyme slows down lactic acid release from muscle cells by the mechanism just discussed, which results in a diminished arteriovenous difference of lactate in the blood.

Carbonic anhydrase activity inside the red blood cell is of minor importance but does have a small effect (dotted curve in Fig. 11). The cause underlying this effect is that in the presence of CA in erythrocytes, more HCO$_3^-$ and H$_3^+$ are produced within red blood cells from CO$_2$ taken up. The H$_3^+$ are buffered by hemoglobin, and part of the HCO$_3^-$ is released from the erythrocytes into the plasma. Accordingly, the pH of plasma within the capillary and also the pH of the interstitial space are slightly more alkaline (calculated under these conditions by 0.04 and 0.03 units, respectively) than in the absence of CA in erythrocytes. The more alkaline pH of the interstitial space enhances lactate-H$_3^+$ co-transport and thus increases the arteriovenous difference of lactate.

Carbonic anhydrase activity in the capillary plasma has no apparent effect on lactate release at all (dashed curve in Fig. 11).

Thus the CA isozyme relevant for lactic acid excretion is almost exclusively the sarcolemmal extracellular CA.

It may be noted that the effect of interstitial CA on lactate release seen in Figure 11 critically depends on the pH dependence of the H$_3^+$-lactate cotransporter and will increase when the pH dependence is greater than assumed here. More importantly, the calculation of Figure 11 is valid only under steady-state conditions, and the role of sarcolemmal CA for lactic acid release is expected to become much greater under non-steady-state conditions. Kowalchuk et al. (106) have indeed made their observations on the inhibitory effect of acetazolamide on lactate uptake by the blood in a non-steady-state situation, immediately after a 30-s period of maximal exercise.

FIG. 11. Effect of carbonic anhydrase (CA) activity in erythrocytes, capillary plasma, or interstitium, respectively, on arteriovenous concentration difference of lactate (avd). CA activity was varied in one compartment, while the activity in the two other compartments was high enough to be not limiting (CA in erythrocytes, $A = 10,000$; CA in capillary, $A = 1,000$; CA on sarcolemma, $A = 1,000$). Conditions chosen for the calculation were as follows: intramuscular $P_{CO_2} = 7.3$ kPa (55 mmHg); intramuscular lactate concentration, 40 mM; arterial lactate concentration, 2 mM. It can be concluded from the figure that it is essentially only the sarcolemmal, interstitial CA that affects lactate release from muscle.
5. Possible physiological role of the plasma inhibitor of CA

The plasma inhibitor makes sure that any activity of CA released from hemolysed erythrocytes is suppressed in the plasma. The physiological role of this plasma inhibitor of CA, which is found in several species, is not known.

One attempt at an explanation could be that a rapid pH equilibration of the blood within the capillary, as it is achieved by the presence of CA in the capillary plasma, is not useful in some species for the following reason. When pH equilibrium is not achieved in the capillary and all the \( \text{H}^+ \) formed are still inside the red blood cells (with the consequence of a slow acid postcapillary pH shift), then a maximum Bohr effect of hemoglobin is achieved and a maximum of \( \text{O}_2 \) should be released from the red blood cells during capillary transit. This may be generally useful to maximize \( \text{O}_2 \) supply to the tissue and may be particularly important in fishes that require high rates of \( \text{O}_2 \) secretion in the swim bladder or the rete mirabile of the eyes. The plasma inhibitor according to this idea would inhibit plasma CA and optimize \( \text{O}_2 \) unloading in all tissues that do not have an intracapillary CA. Tissues that require optimization of their \( \text{CO}_2 \) elimination rather than their \( \text{O}_2 \) supply may then be equipped with an intracapillary CA, making this enzyme available in that organ only.

This prompted us to calculate what effect the presence of CA activity in the capillary plasma has on intracellular pH of erythrocytes within the capillary. Figure 12 shows that in principle this effect does indeed occur; in the absence of capillary CA, endcapillary pH of the intraerythrocytic cytoplasm is \(-0.02\) units lower than in the presence of a capillary CA activity of 20 or more. These calculations were performed for conditions of a high intramuscular \( \text{PCO}_2 \) (\(-8\) kPa; \(60\) mmHg) and high lactate concentration (40 mM), but also with a low lactate excretion and with a \( \text{PCO}_2 \) of \(-7.3\) kPa (\(55\) mmHg), the result is qualitatively similar. Thus plasma inhibitor of CA in principle contributes to tissue oxygenation by decreasing intracellular pH beyond its equilibrium value during capillary passage. This decrease in pH will increase the Bohr effect. However, as is apparent from Figure 12, the effect calculated here is rather small and will improve \( \text{O}_2 \) unloading very little. It thus appears unlikely that this is a major physiological purpose of the plasma inhibitor.

Another possible function of a plasma CA inhibitor emanates from the studies of Wood and Munger (186) on the effect of CA injection into the circulation on the stimulation of ventilation after exhaustive exercise in rainbow trout. These authors found that CA added to the plasma caused a very significant increase in arterial pH and decrease in arterial \( \text{PCO}_2 \) at rest and more so after exhaustive exercise. In the postexercise period, elevated arterial pH and decreased arterial \( \text{PCO}_2 \) resulted in a reduced postexercise hyperventilation, decreased postexercise \( \text{O}_2 \) uptake, and decreased arterial \( \text{PCO}_2 \). Thus, in the postexercise situation, \( \text{CO}_2 \) release appeared to be optimized by plasma CA, but this occurred at the expense of decreased ventilatory drive and decreased \( \text{O}_2 \) supply. Thus, under the aspect of the ventilatory drive exerted by \( \text{PCO}_2 \), it may be useful to suppress any plasma CA in the circulatory system by a plasma inhibitor. It would be desirable to do experiments analogous to those of Wood and Munger (186) in a mammalian system.

V. APPENDIX

This appendix illustrates the equations used for the mathematical model.

A. Interstitial Concentrations of \( \text{CO}_2 \), \( \text{HCO}_3^- \), \( \text{H}^+ \), and Lactate

The transit time necessary for the blood to travel through a capillary is divided into small time steps. During
each time step, blood faces a small part of the interstitial space. For steady-state conditions, interstitial concentrations of lactate, HCO₃⁻, CO₂, and H⁺ were assumed to be stable within this small part. Thus, for one species, the sum of all changes within the interstitial space, i.e., influx and efflux into this space and in the case of CO₂, HCO₃⁻, and H⁺ its forward and backward reaction, has to be zero. For each time step of the blood, the four unknown interstitial concentrations in the small part of the interstitial space are calculated using four equations (Eqs. A1—A4). Concentrations of plasma were taken from the preceding time step, and muscle concentrations were assumed to be constant. Thus a concentration profile for the interstitial space along the capillary is calculated.

For CO₂

\[ 0 = ([CO₂]_{\text{sm}} - [CO₂]_p) \times \frac{P_{CO₂} \times A_{SL}}{\text{vol}_i \times 1,000} - ([CO₂]_p \times P_{CO₂} \times A_{Kap} \times \text{vol}_i) - CA_i \times \left( k_{CO₂} \times [CO₂]_i \right) - k_{H_{CO₂}} \times \frac{[H^+] \times [HCO₃^-]}{K_1} \] (A1)

For HCO₃⁻

\[ 0 = CA_i \times \left( k_{CO₂} \times [CO₂]_i - k_{H_{CO₂}} \times \frac{[H^+] \times [HCO₃^-]}{K_1} \right) - ([HCO₃^-]_i - [HCO₃^-]_p) \times \frac{P_{HCO₃} \times A_{Kap}}{\text{vol}_i} \] (A2)

For H⁺

Lactate and H⁺ are transported equimolar across the sarcolemma; thus for H⁺ flux across this membrane, the same term is used for lactate and H⁺. H⁺ transport out of the muscle cell by other transporters is neglected.

\[ 0 = \left( \frac{[La^-]_{\text{sm}} \times V_{\text{max}}}{K_m + [La^-]_{\text{sm}}} - \frac{[La^-]_i \times V_{\text{maxR}}}{K_m + [La^-]_i} \right) \times \frac{A_{SL}}{\text{vol}_i} + CA_i \times \left( k_{CO₂} \times [CO₂]_i - k_{H_{CO₂}} \times \frac{[H^+] \times [HCO₃^-]}{K_1} \right) - ([H^+]_i - [H^+]_p) \times \frac{P_{H^+} \times A_{Kap}}{\text{vol}_i} \] (A3)

For lactate

\[ 0 = \left( \frac{[La^-]_{\text{sm}} \times V_{\text{max}}}{K_m + [La^-]_{\text{sm}}} - \frac{[La^-]_i \times V_{\text{maxR}}}{K_m + [La^-]_i} \right) \times \frac{A_{SL}}{\text{vol}_i} - ([La^-]_i \times \frac{P_{La} \times A_{Kap}}{\text{vol}_i}) \] (A4)

Dependence of H⁺-lactate cotransport on pH was assumed to be linear for the relevant pH range. With a decrease of pH from 7.4 by one unit, lactate flux decreases to a fraction (V_r) of the flux at pH 7.4 (calculated as in Ref. 93)

\[ V_{\text{max}} = V_{\text{max,7.4}} \times \{1 - V_r(7.4 + \log_{10}[H^+]) - 3\} \]

\[ V_{\text{maxr}} = V_{\text{max,7.4}} \times [1 - V_r(7.4 - \text{pH}_{\text{sm}})] \]

B. Concentration Changes Within Plasma and Erythrocytes

Concentration changes are calculated for erythrocytes and plasma as blood flows along the capillary wall using the interstitial concentration as calculated above for each time step.

1. CO₂

\[ \frac{d[C_{O₂}]_e}{dt} = \left( -k_{CO₂} \times [C_{O₂}]_e + k_{H_{CO₃}} \times \frac{[H^+]_e \times [HCO₃^-]_e}{K_1} \times CA_e - \frac{d[\text{carb}]}{dt} \right) + ([C_{O₂}]_p - [C_{O₂}]_e) \times \frac{P_{CO₂} \times A_e}{\text{wvol}_e} \] (A5)

2. Carbamate

With the assumption of constant blood flow, no anoxic regions, and constant O₂ consumption within muscle tissue along the capillary, it follows that O₂ flow across the capillary wall should be constant for each part of the capillary. Thus deoxygenation of hemoglobin during capillary passage was assumed to increase linearly along the capillary.

\[ [Hb] = [Hb]_0 + \frac{t}{TZ} \times ([Hb]_{\text{end}} - [Hb]_0) \]
The actual carboxylate concentration converges during each time step toward an equilibrium concentration determined by the actual concentration of CO\(_2\), pH and actual saturation of hemoglobin with a half-time \(t_{1/2}\).

\[
\frac{d[\text{carb}]}{dt} = \ln 2 \times \left(\frac{[\text{Hb}]_{\text{oxy}} \times z_o}{2} + [\text{Hb}] \times z_r - [\text{Carb}]_{\text{alt}}\right)
\]

\[
z_o = \frac{2 \times [\text{CO}_2]_e}{4 \times \left[\frac{[\text{CO}_2]_e + [\text{H}^+]_e + [\text{H}^+]_p}{K_{c,\text{oxy}} + K_{c,\text{oxy}} \times K_{c,\text{oxy}}}\right]}
\]

3. Membrane potential

\[
E = -\frac{R \times T}{P} \left[\frac{2}{u_{\text{Cl}_-} \times [\text{Cl}^-]_p + u_{\text{HCO}_3^-} \times [\text{HCO}_3^-]_p + u_{\text{lact}^-} \times [\text{lact}^-]_p + u_{\text{cation}} \times [\text{cation}]_p}{\ln \left(\frac{2}{u_{\text{Cl}_-} \times [\text{Cl}^-]_p + u_{\text{HCO}_3^-} \times [\text{HCO}_3^-]_p + u_{\text{lact}^-} \times [\text{lact}^-]_p + u_{\text{cation}} \times [\text{cation}]_p}\right) - \ln \left(\frac{1}{u_{\text{Cl}_-} \times [\text{Cl}^-]_p + u_{\text{HCO}_3^-} \times [\text{HCO}_3^-]_p + u_{\text{lact}^-} \times [\text{lact}^-]_p + u_{\text{cation}} \times [\text{cation}]_p}\right)}\right]
\]

3. HCO\(_3\)^-

\[
\frac{d[\text{HCO}_3^-]_p}{dt} = \left(k_{\text{CO}_2} \times [\text{CO}_2]_p - k_{\text{H}_2\text{CO}_3}\right) \times \left(\frac{[\text{H}^+]_p \times [\text{HCO}_3^-]_p}{K_1}\right) \times \left[C\text{Ap} + \frac{\Phi_{\text{HCO}_3^-} \times A_{\text{Kap}}}{\text{vol}_p}\right]
\]

\[
\frac{d[\text{HCO}_3^-]_e}{dt} = \left(k_{\text{CO}_2} \times [\text{CO}_2]_e - k_{\text{H}_2\text{CO}_3}\right) \times \left(\frac{[\text{H}^+]_e \times [\text{HCO}_3^-]_e}{K_1}\right) \times \left[C\text{Ap} + \frac{\Phi_{\text{HCO}_3^-} \times A_{\text{Kap}}}{\text{vol}_e}\right]
\]

4. H\(^+\)

\[
\frac{d[\text{H}^+]_p}{dt} = \frac{\ln 10 \times [\text{H}^+]_p}{\beta_p} \times \left(1 - \frac{k_{\text{CO}_2} \times [\text{CO}_2]_p - k_{\text{H}_2\text{CO}_3}}{K_1}\right) \times \left[C\text{Ap} + \frac{\left[d[\text{H}^+]_p\right]}{dt} + \left([\text{H}^+]_p\right) \times \left[\frac{P_{\text{H}^+} \times A_{\text{Kap}}}{\text{vol}_p}\right]\right]
\]

\[
\frac{d[\text{H}^+]_e}{dt} = \frac{\ln 10 \times [\text{H}^+]_e}{\beta_e} \times \left(1 - \frac{k_{\text{CO}_2} \times [\text{CO}_2]_e - k_{\text{H}_2\text{CO}_3}}{K_1}\right) \times \left[C\text{Ap} + \frac{\left[d[\text{carb}\right]}{dt} + \left([\text{H}^+]_e\right) \times \left[\frac{P_{\text{H}^+} \times A_{\text{Kap}}}{\text{vol}_e}\right]\right]
\]

\[
\Phi_{\text{HCO}_3^-} = \frac{u_{\text{HCO}_3^-} \times E \times A_e}{d_e}
\]

\[
\times \left(\frac{\left[HCO_3^-\right]_p - \left[HCO_3^-\right]_e \times e^{(E \times F)(R \times T)}}{1 - e^{(E \times F)(R \times T)}}\right) \times (\text{mmol} \cdot L^{-1} \cdot s^{-1})
\]

5. Lactate, lactic acid, and lactic acid contribution to H\(^+\)

Step 1 is change of lactate ion concentration and lactic acid concentration.
\[ \frac{\Delta [\text{La}^-]}{dt} = -\frac{\Phi_{\text{La}^-}}{\text{vol}_p} + ([\text{La}^-]_i - [\text{La}^-]_p) \times P_{\text{La}^-} \times \frac{A_{\text{Kap}}}{\text{vol}_p} \]

\[ \frac{\Delta [\text{La}^-]}{dt} = + \frac{\Phi_{\text{La}^-}}{\text{wvol}_e} \]

H\textsuperscript+ /H\textsuperscript− cotransport and nonionic diffusion were regarded together as change in lactic acid (HLa) concentration

\[ \frac{\Delta [\text{HLa}]}{dt} = ([\text{HLa}]_p - [\text{HLa}]_e) \times P_{\text{HLa}} \times \frac{A_e}{\text{wvol}_e} \]

\[ = \left( \frac{[\text{La}^-] \times V_{\text{max,e}}}{K_{\text{m,e}} + [\text{La}^-]} \right) \times \frac{A_e}{\text{wvol}_e} \]

\[ \frac{\Delta [\text{HLa}]}{dt} = -([\text{HLa}]_p - [\text{HLa}]_e) \times P_{\text{HLa}} \times \frac{A_e}{\text{vol}_p} + ([\text{HLa}]_i - [\text{HLa}]_p) \times P_{\text{La}^-} \times \frac{A_{\text{Kap}}}{\text{vol}_p} - \frac{[\text{La}^-] \times V_{\text{max,e}}}{K_{\text{m,e}} + [\text{La}^-]} \times \frac{A_e}{\text{vol}_p} \]

\[ \times [\text{La}^-] \times V_{\text{max,e}} \times \frac{A_e \times 1,000}{\text{wvol}_e} \]

Step 2 is equilibration between lactic acid and lactate. After this change in the concentration of lactate ions and lactic acid during the small time step \( dt = \Delta t (<1 \text{ ms}) \), an equilibrium between these forms is immediately achieved. As a result, dissociation of lactic acid will increase equimolarly and simultaneously the concentration in lactate and H\textsuperscript{+}.

\[ [\text{H}^+] \times [\text{La}^-] = K_{\text{lactic acid}} \times [\text{HLa}] \]

Taking derivatives on both sides gives

\[ \frac{d[\text{H}^+]}{dt} \times [\text{La}^-] + [\text{H}^+] \times \frac{d[\text{La}^-]}{dt} = K_{\text{lactic acid}} \times \frac{d[\text{HLa}]}{dt} \]

With substituting in this equation

\[ \frac{d[\text{HLa}]}{dt} = \frac{\Delta [\text{HLa}]}{dt} - \frac{d[\text{H}^+]_{\text{la}}}{dt} \]

and solving for \( d[\text{H}^+]_{\text{la}}/dt \), this gives

\[ \frac{d[H^+]_{\text{la}}}{dt} = \frac{\Delta [\text{HLa}]}{dt} \times \frac{K_{\text{lactic acid}} \times [\text{HLa}]}{[\text{La}^-] + [\text{H}^+] + K_{\text{lactic acid}}} \]

For plasma and erythrocytes, the appropriate indexes are to be used.

C. Volumes

volumes: whole blood = \( 1 = \text{vol}_p + 0.72 \times \text{vol}_e \)

\[ \text{wvol}_e = \text{vol}_e \times 0.72 \]

interstitial space, \( \text{vol}_i = 2 \)

Flux of water is described only across the erythrocytic membrane using a hydraulic permeability coefficient and the difference in osmolarity using the equations by Bidani et al. (10), and thus changes of volume are calculated for red blood cells and plasma only.

\[ \frac{dwvol_e}{dt} = L_p \times (\text{osm}_e - \text{osm}_p) \times A_e \times V_w \text{ (s}^{-1}\text{)} \]

\[ \text{wvol}_{e,\text{neu}} = \Delta t \times \frac{dwvol_e}{dt} + \text{wvol}_{e,\text{alt}} \]

\[ \text{vol}_{p,\text{neu}} = 1 - 	ext{wvol}_{e,\text{neu}} - 0.28 \times \text{vol}_e \]

\[ = -\Delta t \times \frac{dwvol_e}{dt} + \text{vol}_{s,\text{alt}} \]

After calculations for each time step were finished, concentrations in erythrocytes and plasma were multiplied with dilution factors.

\[ VF_e = \frac{\text{wvol}_{e,\text{alt}}}{\text{wvol}_{e,\text{neu}}} = \frac{\text{wvol}_{e,\text{alt}}}{\text{wvol}_{e,\text{alt}} + \Delta t \times \frac{dwvol_e}{dt}} \]

\[ VF_p = \frac{\text{vol}_{p,\text{alt}}}{\text{vol}_{p,\text{neu}}} = \frac{\text{vol}_{p,\text{alt}}}{\text{vol}_{p,\text{alt}} - \Delta t \times \frac{dwvol_e}{dt}} \]

D. Solutions

The changes in erythrocytic and plasma concentrations during capillary transit were observed solving all
equations numerically for small time steps (usually 0.75 ms) after calculating for each time step the concentrations in the respective small part of the interstitial space. For postcapillary conditions, equations concerning movement out of muscle and interstitial space were removed and time steps were longer.

The programs were written in C (Borland, Vs 3.1) on a personal computer with the help of Dr. Reinhard Knörr, Institute of Mathematics, University of Rostock, Rostock, Germany.

E. Indexes Used

alt in the preceeding time step
e erythrocyte
i interstitial space
Kap capillary wall
neu in the actual time step
p plasma
SL sarcolemma
sm skeletal muscle cell

e. Abbreviations and Values of Parameters Used

$A_e$ (7,800 cm$^2$/cm$^3$ blood) surface of erythrocytes/ml blood

$A_{Kap}$ (5,700 cm$^2$/cm$^3$ Blut) surface capillary wall/ml blood

$A_{SL}$ (2.85 × 10$^7$ cm$^2$/l blood) surface of sarcolemma/liter blood (=5 times $A_{Kap}$)

CA (varied) carbonic anhydrase activity, factor by which the uncatalyzed reaction is accelerated

[Carb] carbamate concentration
d$_c$ (10$^{-6}$ cm) thickness of erythrocyte membrane

$E$ (-9 mV) membrane potential of erythrocytes

$F$ (96,480 C/mol) Faraday constant

$[Hb]$ actual concentration of deoxygenated hemoglobin

$[Hb]_{end}$ concentration of deoxygenated hemoglobin in venous blood

$[Hb]_i$ concentration of deoxygenated hemoglobin in arterial blood

$[Hb]_{oxy}$ actual concentration of oxygenated hemoglobin

$[HLa]$ lactic acid concentration

$K_m$ (23.7 mM) H$^+$-lactate cotransport, skeletal muscle of rats (91)

$K_{m,e}$ (15 mM) H$^+$-lactate cotransport, estimate for erythrocytes (138)

$k_{CO_2}$ (0.13 s$^{-1}$) CO$_2$ hydration velocity constant

(taken from Ref. 10)

$k_{HCO_3}$ (57.5 s$^{-1}$) H$_2$CO$_3$ dehydratons velocity constant

(taken from Ref. 10)

$K_1$ (0.35 mM) acid dissociation constant for H$_2$CO$_3$

(taken from Ref. 10)

$K_{lactic}$ acid (10$^{-0.36}$ mM) equilibrium constant for lactic acid

$K_{c,oxy}$ $K_{z,oxy}$ $K_{c,at}$ $K_{z,at}$ $K_{c,\beta}$ $K_{z,\beta}$ binding constants for carbamate (see sect. II)

$L_p$ (0.041 cm/s) bovine red cell hydraulic coefficient

(taken from Ref. 10)

osm osmolarity

$P_{CO_2}$ (1 cm/s) permeability of membranes for CO$_2$

$P_{HCO_3}$ 3.7 × 10$^{-5}$ cm/s lactic acid permeability, erythrocytes 30°C (27)

$P_{CO_3}$, $P_{H^+}$, $P_{La^-}$ (varied) permeability of capillary wall

$R$ (8.314 mJ K$^{-1}$ mol$^{-1}$) universal gas constant

$T$ (310°K) temperature, 310°K (=37°C)

$TZ$ (varied) capillary transit time

t$1/2$ (0.12 s) for carbamate reaction (102)

t actual time after blood has entered the capillary

$u_{CT}$, $u_{HCO_3}$ (2 × 10$^{-11}$ cm$^2$.s$^{-1}$.mV$^{-1}$) ion mobility (calculated from $P_{HCO_3}$ = 5.6 × 10$^{-3}$ cm/s; Ref. 160)

$u_{La}$ (2 × 10$^{-15}$ cm$^2$.s$^{-1}$.mV$^{-1}$) ion mobility for lactate, estimated to be 10,000 lower than $u_{HCO_3}$

vol (volume/volume blood) volume of interstitial space, volume of plasma, volume of erythrocytes

$V_{max,7.4}$ (160 × 10$^{-9}$ mmol · cm$^{-2}$ · s$^{-1}$) maximal lactate flux in sarcolemmal vesicles; estimate for 37°C (from Ref. 91)

$V_{max,e}$ $V_{Max,7.4}$ (2.5 × 10$^{-9}$ mmol · cm$^{-2}$ · s$^{-1}$) maximal lactate flux in erythrocytes (estimate from Ref. 138)

$V_e$ (0.2) fraction to which lactate flux is reduced with pH decrease from 7.4 to 6.4 (estimated from Ref. 93)

$V_w$ (1.809 × 10$^{-5}$ l/mM) millimolar volume of water (37°C)

$wvol_e$ (0.72 × vol$_w$) volume of water within erythrocytes

zo CO$_2$ bound per tetramer oxygenated hemoglobin

$zr$ CO$_2$ bound per tetramer deoxygenated hemoglobin

$\alpha$ [0.0318 mM/(1 × Torr)] solubility coefficient for CO$_2$

$\beta_p$ (5.5 nmol H$^+$/unit pH) nonbicarbonate buffer capacity of plasma ($\beta_i = 0.5\beta_p$)

$\beta_c$ (60 nmol H$^+$/unit pH) nonbicarbonate buffer capacity of erythrocytes

$\vartheta$ (0.7 nmol H$^+$ bound/mmol HbO$_2$ formed) per Hb monomer (taken from Ref. 10)

$\Phi$ anion flux from plasma into erythrocytes

$\gamma$ (1.8 mmol H$^+$ released/mmol Carb formed) (taken from Ref. 10)

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